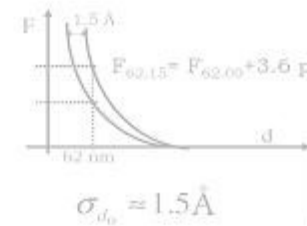
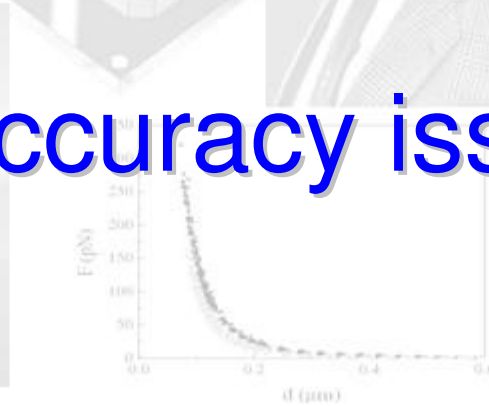
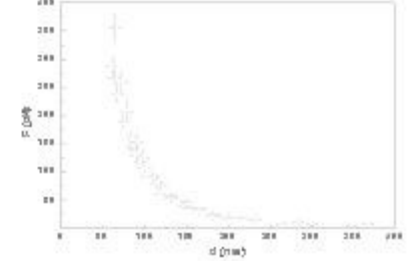


Casimir force experiments:

beyond the accuracy issue



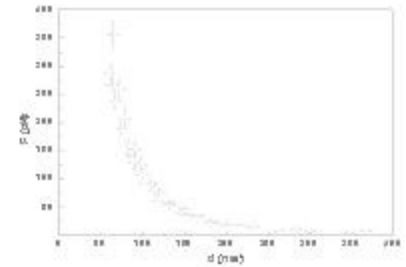
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An interesting (and useful) analogy



P.C.Caussée (1836)
L'Album du Marin

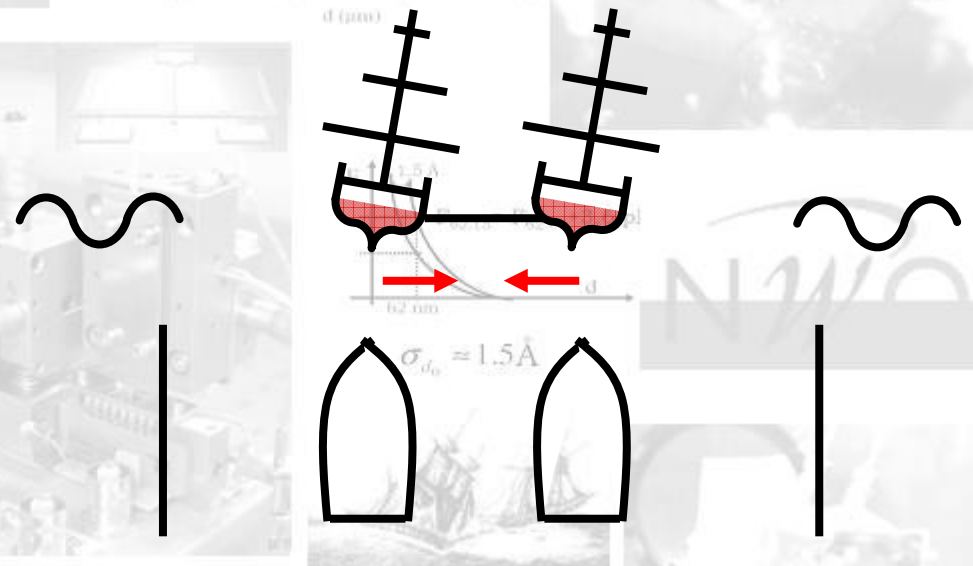


Two ships, standing parallel in the wavy sea, are driven one against the other by a mysterious attractive force

S. L. Boersma
Am. J. Phys. **64** (1996) 539

The two ships act like barriers

They are pushed one against the other by the waves outside "the gap"



The zero-point energy

Maxwell equations

Uncertainty principle

Energy of a mono-chromatic e.m. wave

$$E_n = \hbar \omega \left(n + \frac{1}{2} \right)$$

Vacuum

$$n = 0 \quad \forall \omega$$

$$E_0 = \frac{1}{2} \hbar \omega$$

Vacuum is not empty!

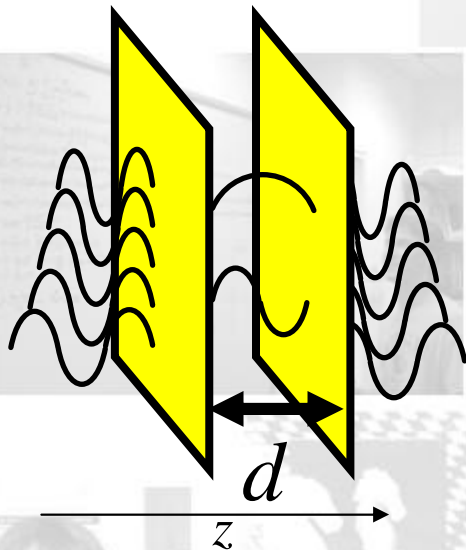
Vacuum is filled with the energy produced by the quantum fluctuations of the electromagnetic field



The Casimir effect

Two metallic parallel plates in vacuum: only some modes can exist

$$E = \sum_{\omega_m} \frac{1}{2} \hbar \omega_m; \quad \omega_m = c \left(k_x^2 + k_y^2 + \frac{\pi^2}{d^2} m^2 \right)^{1/2}$$

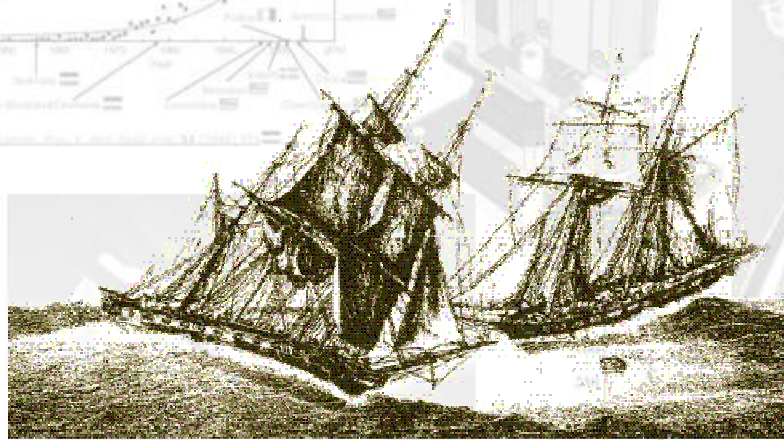


The zero-point energy depends on d , therefore:

$$F = -\frac{\partial E}{\partial d} = -\frac{\pi^2 \hbar c}{240 d^4} L^2$$



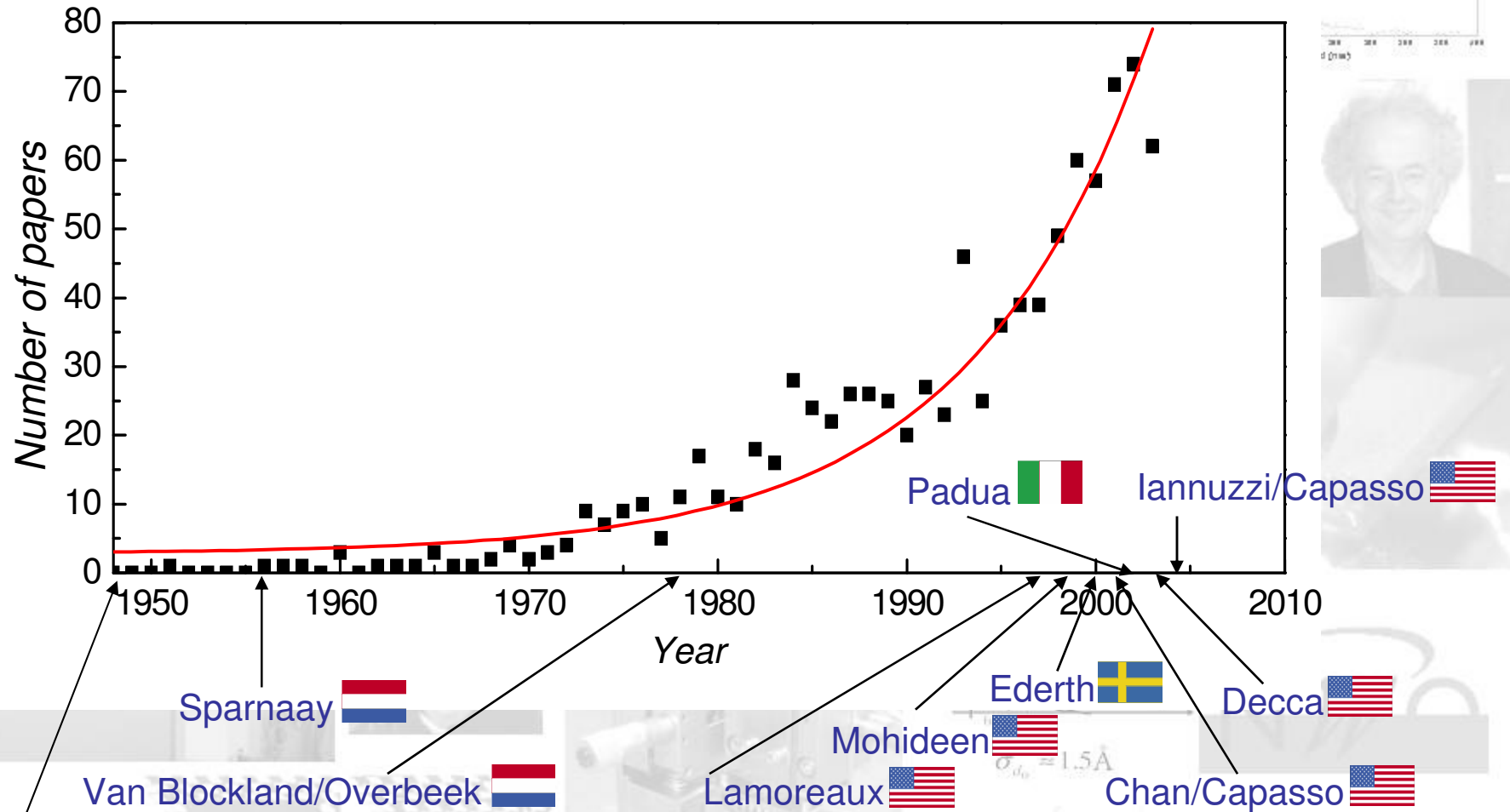
The Casimir effect



The plates act like ships in the wavy sea of electromagnetic quantum fluctuations



The Casimir effect: history of a paper



H. B. G. Casimir, *Proc. K. Ned. Akad. Wet.* **51** (1948) 793 



Reasons of this renewed interest

- The only macroscopic manifestation of QED
- Zero-point energy problem
- Gravitation at short distances, extragravitational forces
- Micro- and Nanotechnologies

$$P = \frac{F}{L^2} = - \frac{\pi^2 \hbar c}{240 d^4}$$

$$P \approx 1 \cdot 10^{-15} \text{ N/m}^2 \text{ at } d=1 \text{ mm}$$

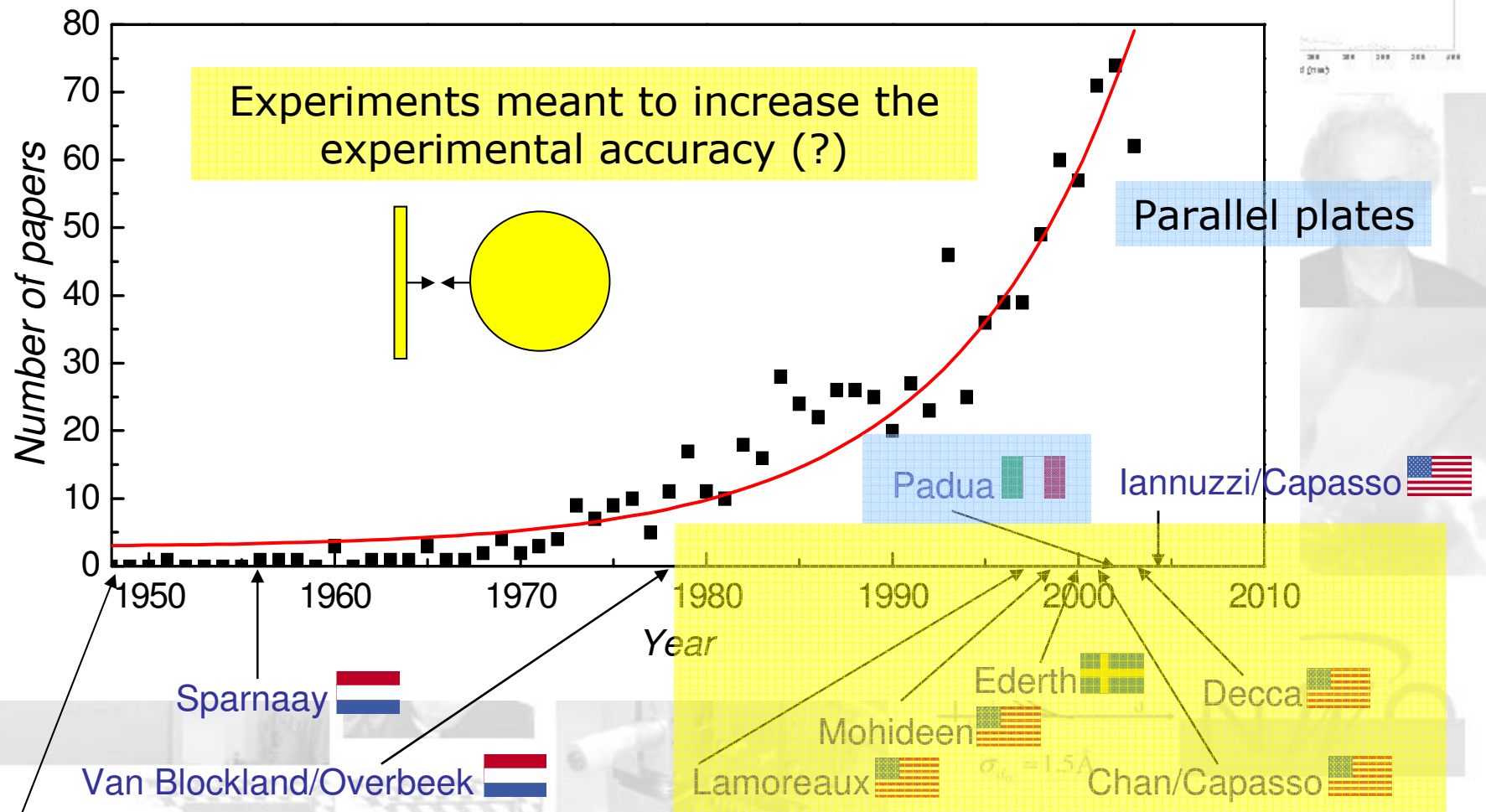
$$P \approx 1 \text{ mN/m}^2 \text{ at } d=1 \mu\text{m}$$

$$P \approx 1 \text{ atm} \text{ at } d=10 \text{ nm}$$

(for ideal metals)



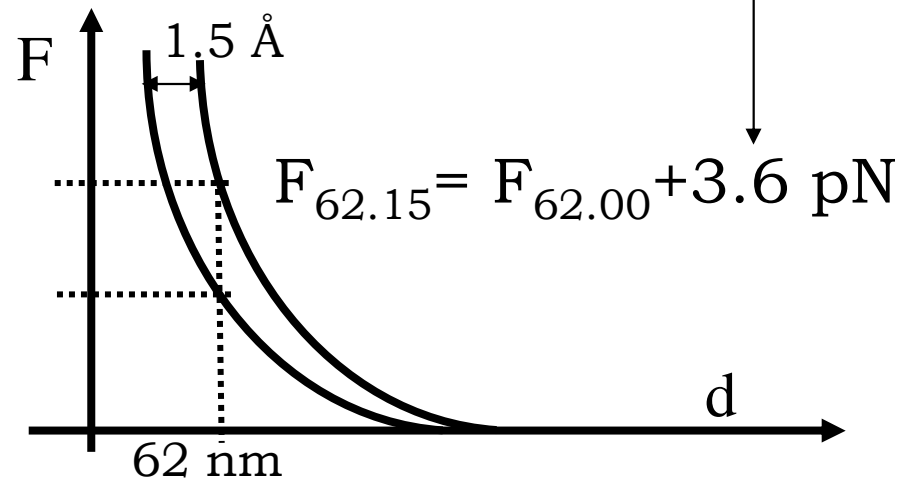
The trend



H. B. G. Casimir, *Proc. K. Ned. Akad. Wet.* **51** (1948) 793

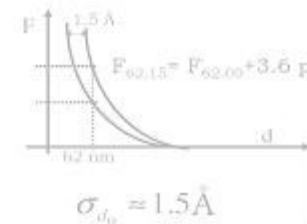


The accuracy issue

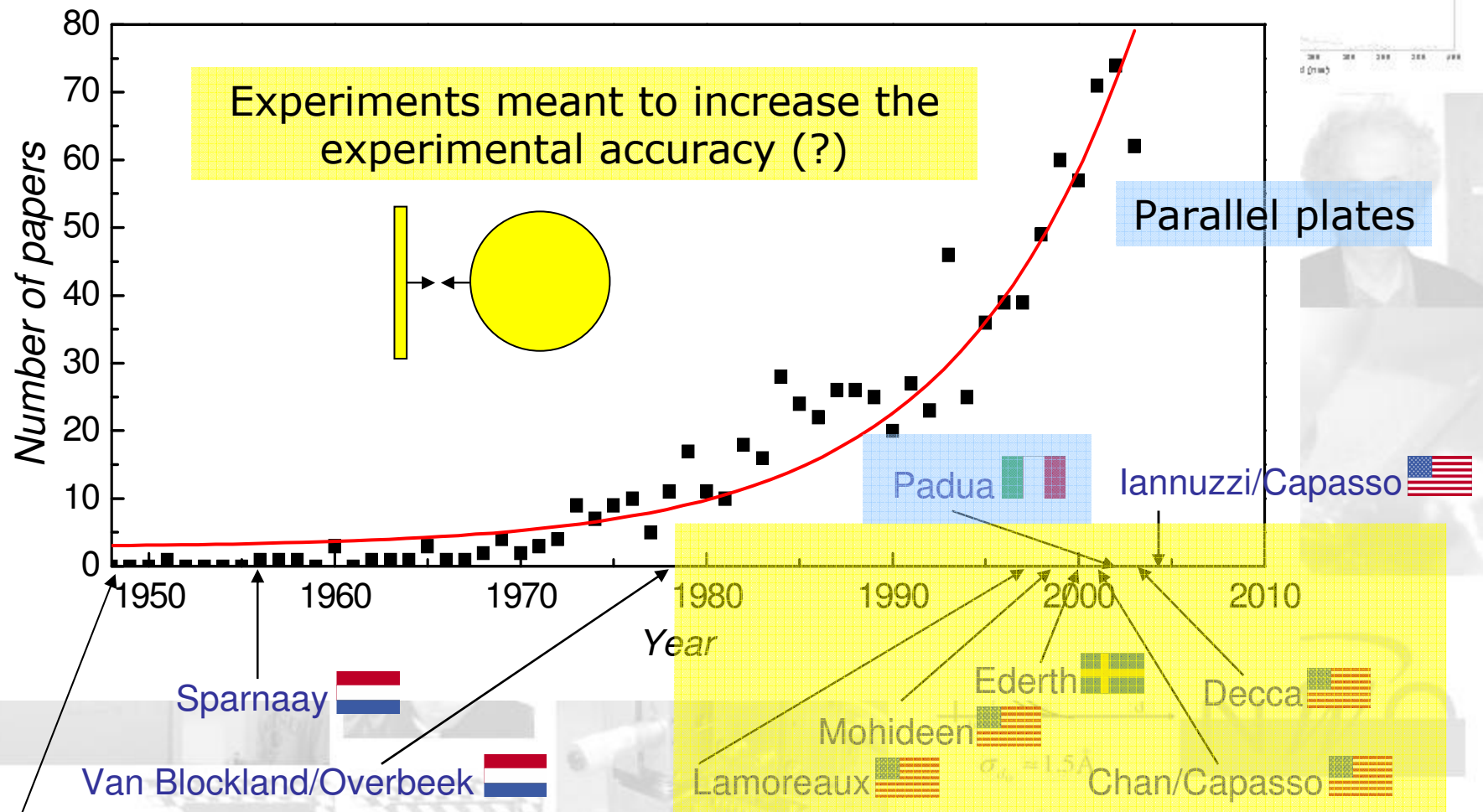


$$\sigma_{d_0} \approx 1.5 \text{ \AA}$$

- No direct measurement of d
- Surface roughness corrections
- Finite conductivity corrections
- Electrostatic under control?



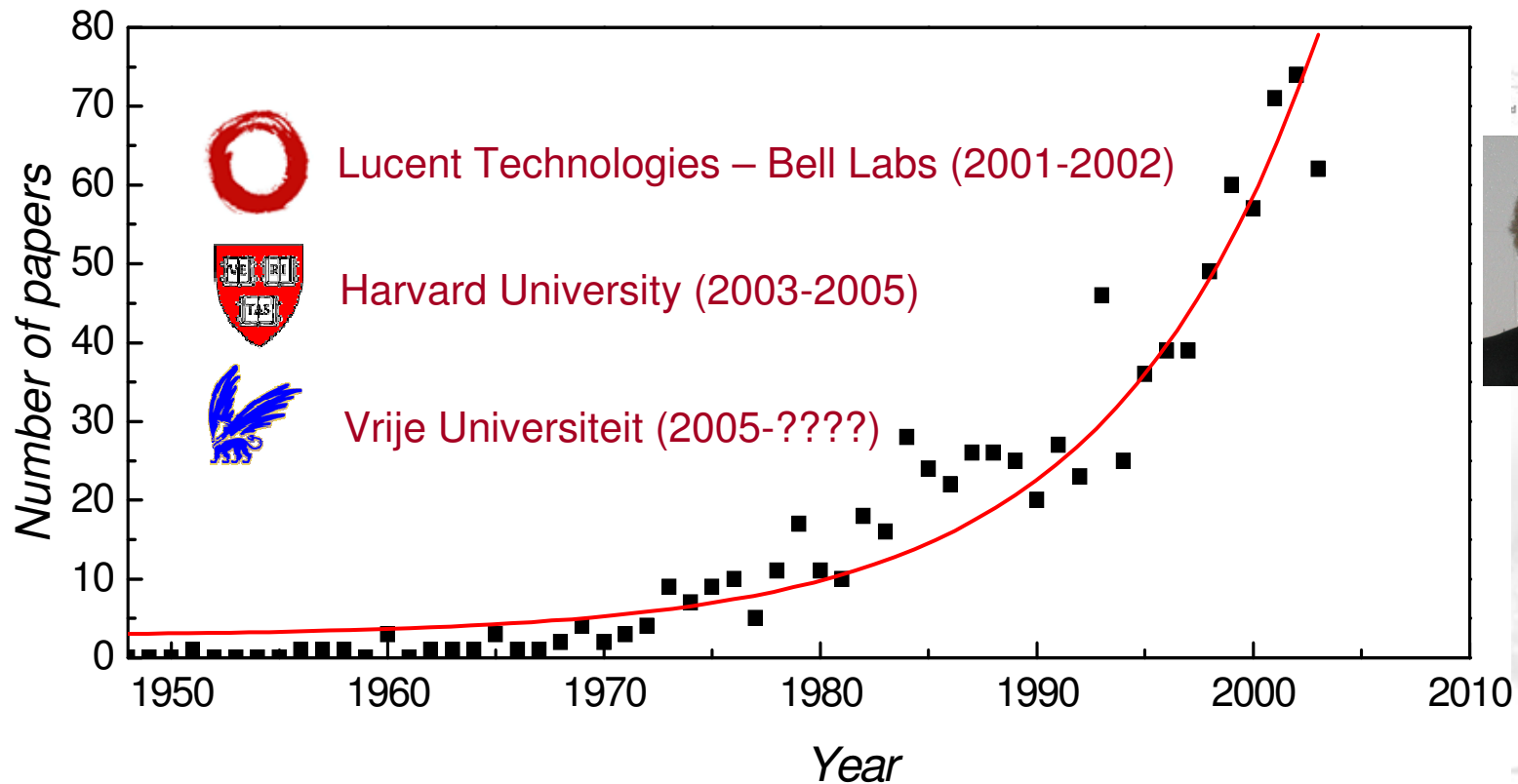
The trend



H. B. G. Casimir, *Proc. K. Ned. Akad. Wet.* **51** (1948) 793



A different approach



QUANTUM FLUCTUATIONS ENGINEERING

Design of the interacting
surfaces



Design of the Casimir
interaction

Review papers:

- Iannuzzi, Lisanti, Munday, Capasso, *Solid State Comm.* **135** (2005) 618
- Iannuzzi, Lisanti, Munday, Capasso, *J. Phys.* **A39** (2006) 6445



Quantum fluctuations engineering

Casimir paper: two **PERFECT CONDUCTORS**

Real materials $\epsilon(\omega)$ $\longleftrightarrow$ Boundary conditions

$\epsilon(\omega) \longleftrightarrow F$ $\longrightarrow$ The Casimir force depends on which materials the interacting surfaces are made of (Lifshitz theory)

Highly reflective

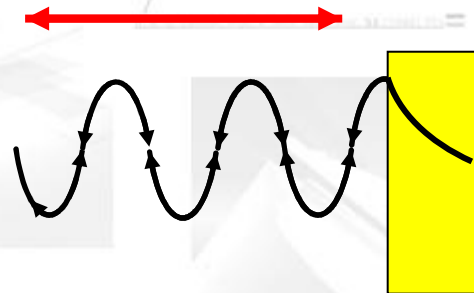
Transparent

Conductive surfaces are needed
(charge accumulation on the surfaces mimics the Casimir effect)

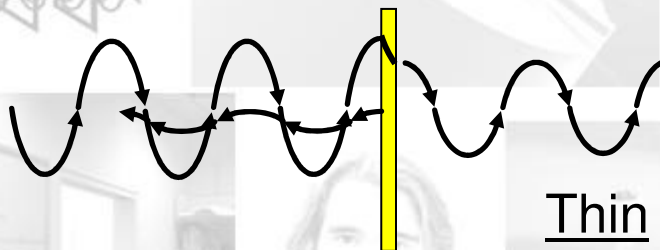


Casimir force: skin-depth effect

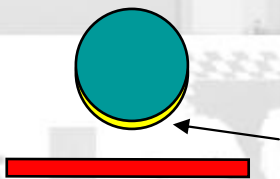
When is a metallic layer really a mirror?



Thick (bulk-like) metallic film: reflective



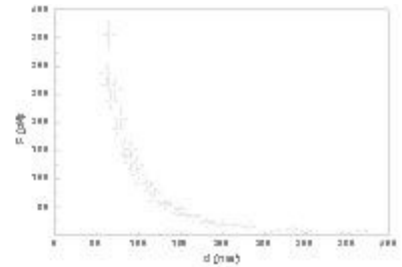
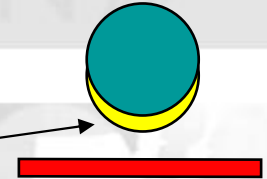
Thin metallic film: transparent
(but still metallic!)



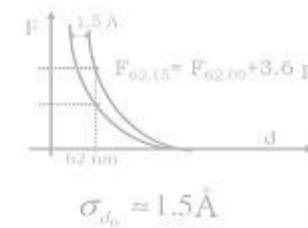
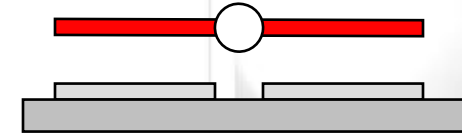
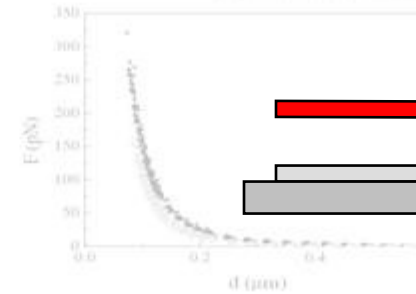
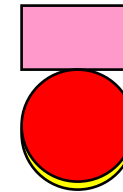
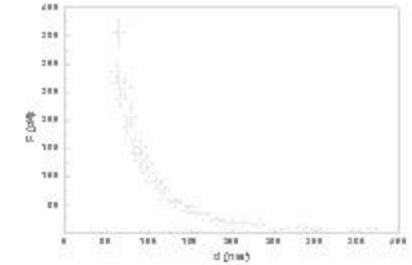
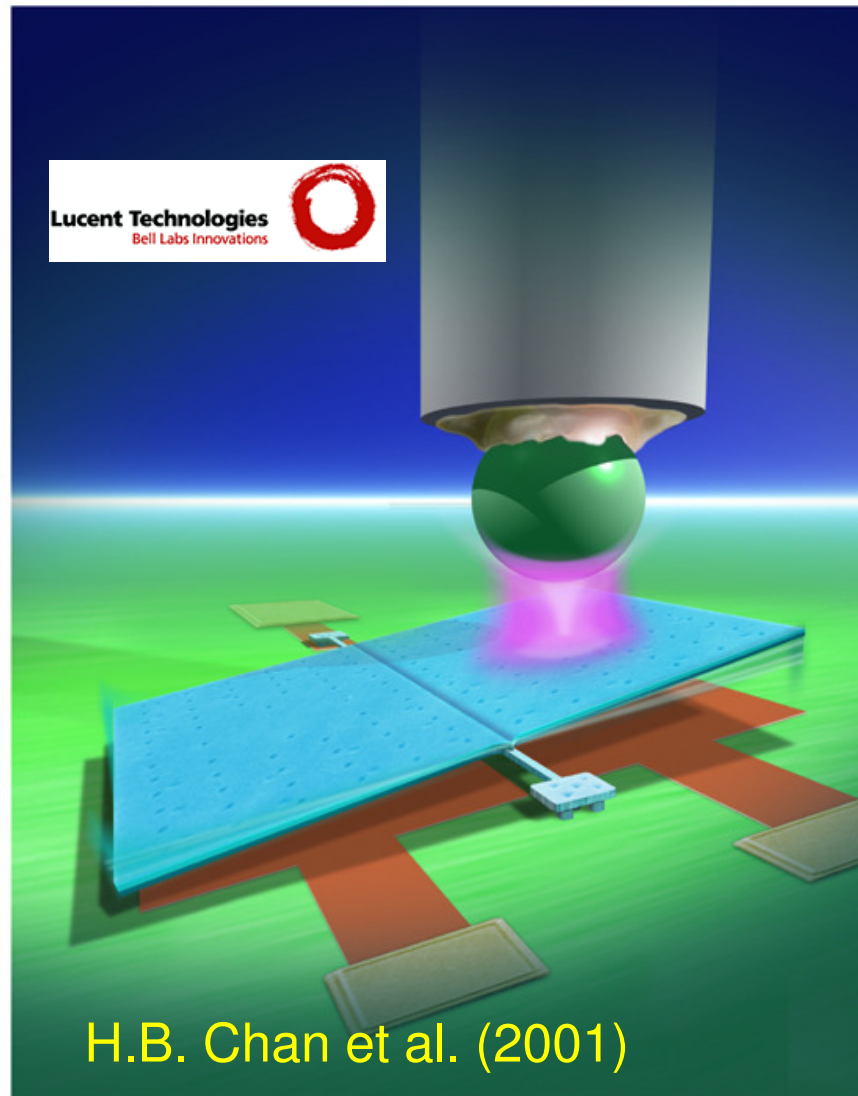
Thin metallic layer

Transparent sphere coated with

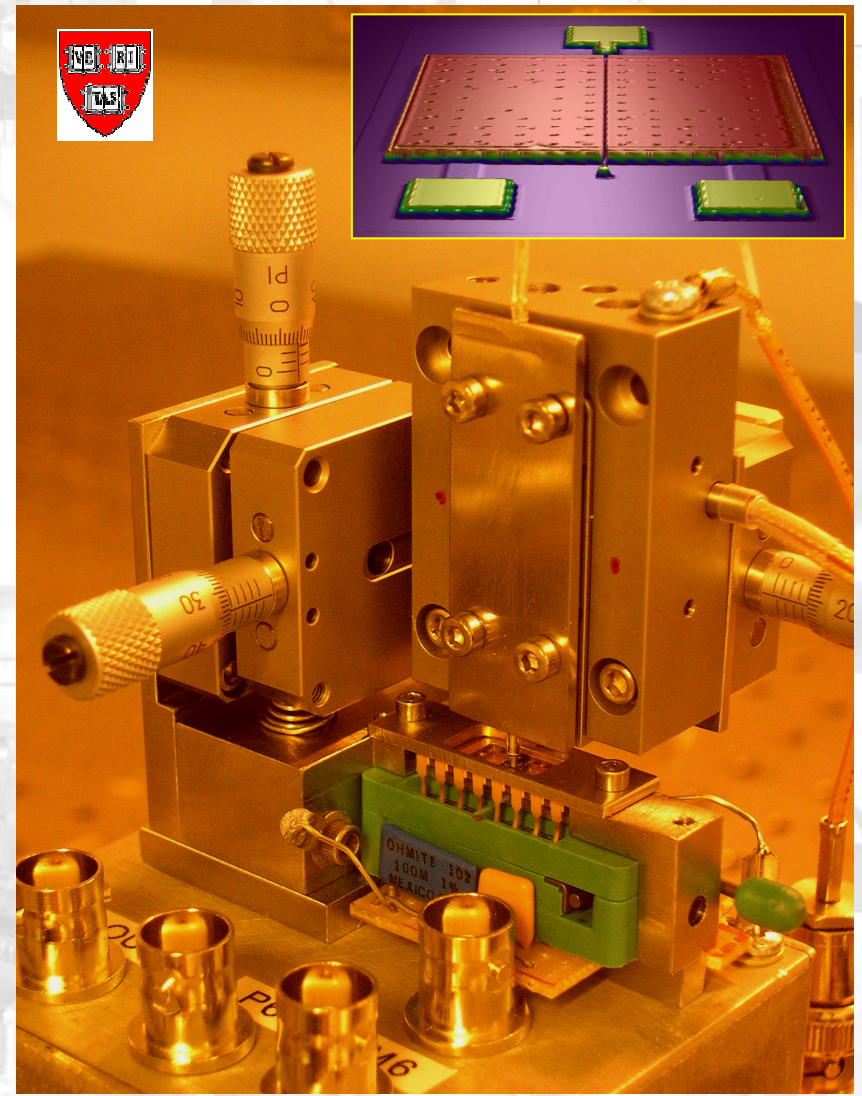
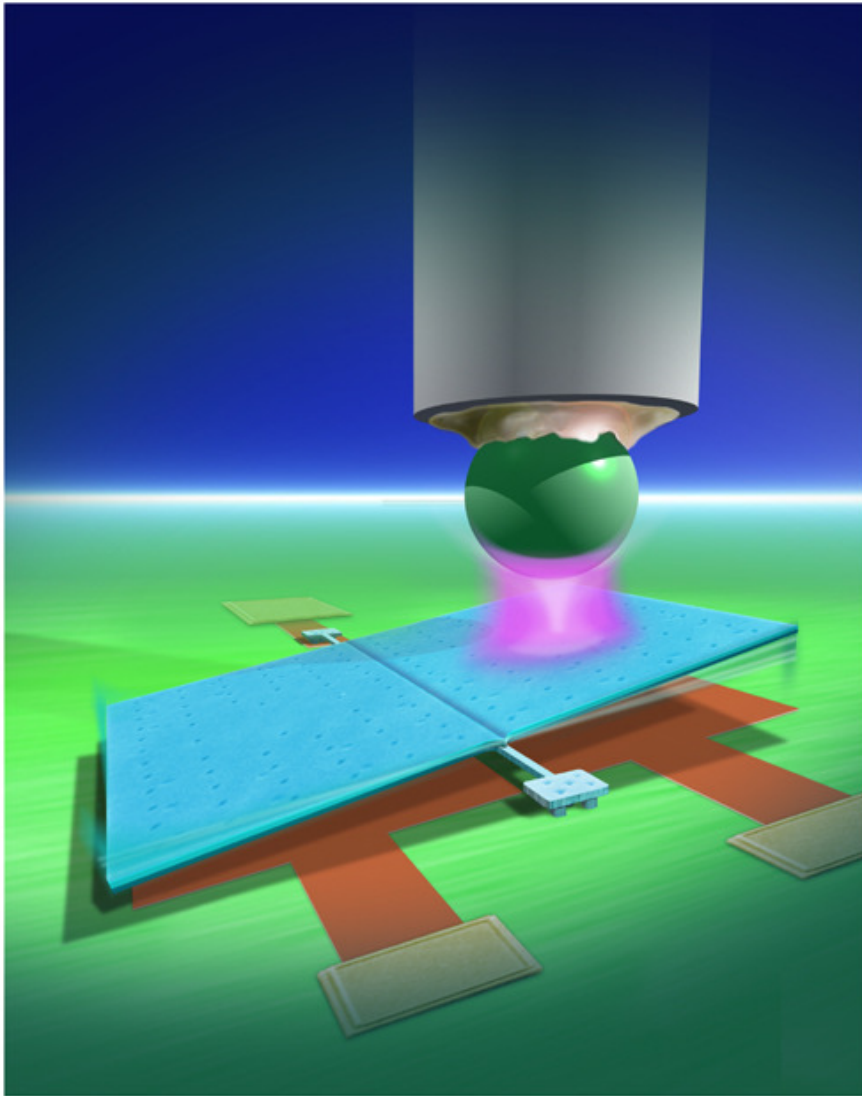
Thick metallic layer



Casimir force: experimental set-up



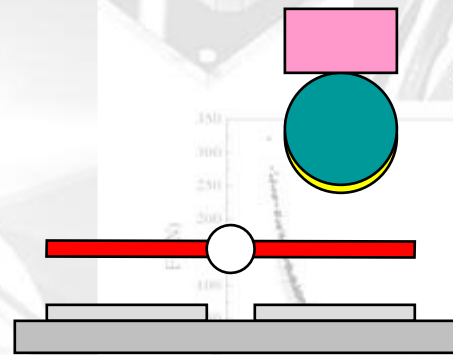
Casimir force: experimental set-up



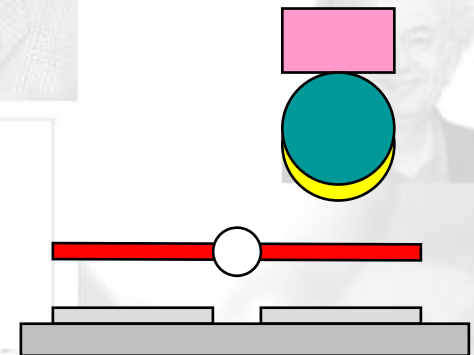
Casimir force: skin-depth effect



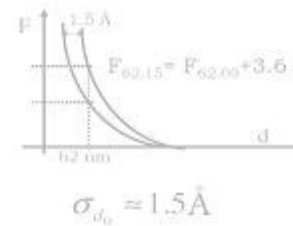
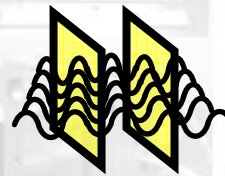
Mariangela Lisanti
(now at Stanford)



Thin film of Pd



Thick film of Pd



Thin and thick film should behave differently:
skin-depth effect in the Casimir force

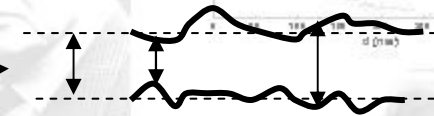


Casimir force: skin-depth effect

Main problems:

- surface roughness
- radius of the sphere

$$F = -\frac{\pi^3 \hbar c}{360 d^3} R$$



1st evaporation
(thin film)

Meas. of surface
roughness

1st Casimir force
meas. (thin film)

-Data with thick film
are taken only if the
surface roughness
is the same

2nd evaporation
(on top of thin film)

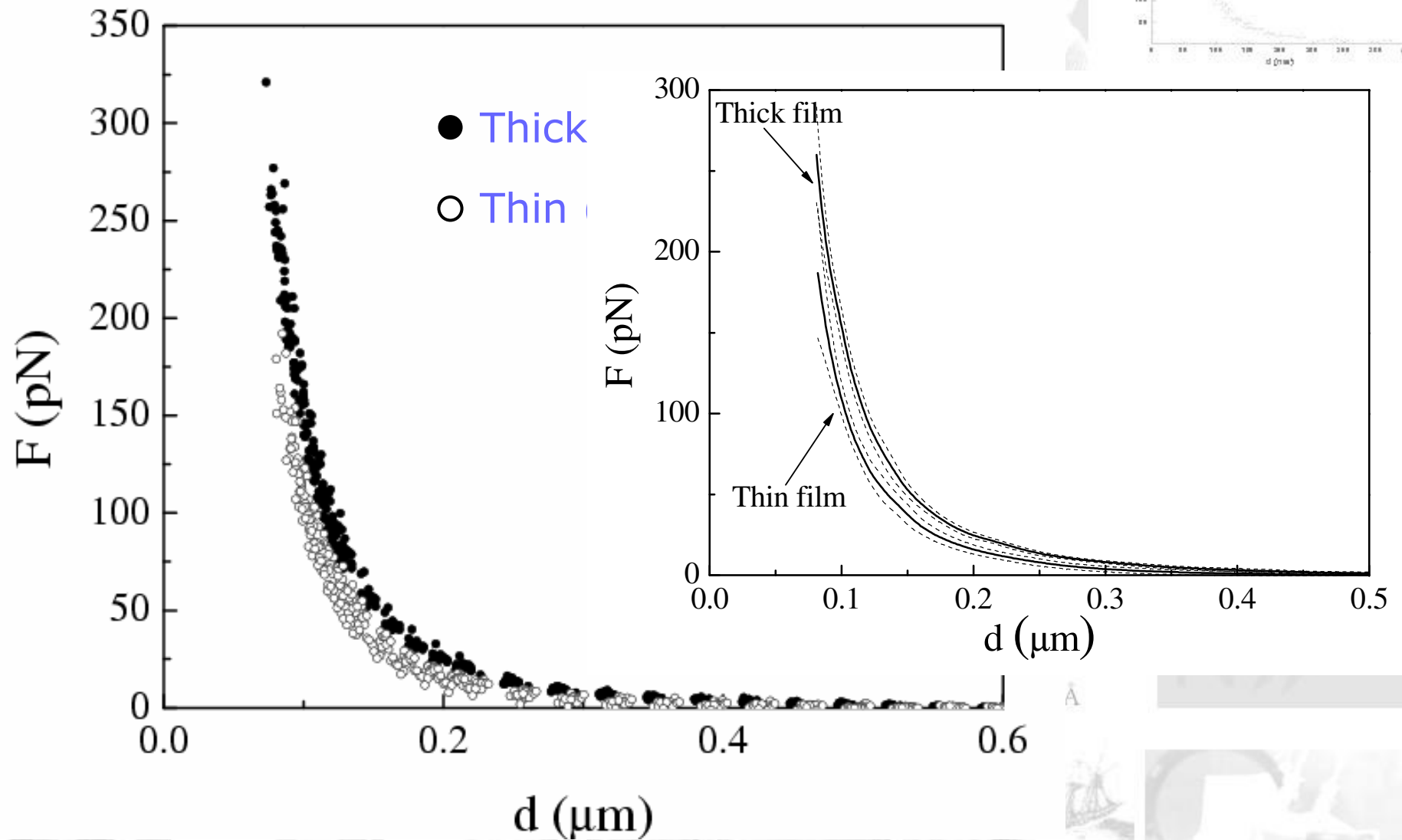
Meas. of surface
roughness

2nd Casimir force
meas. (thick film)

-**Same radius**
because it is the
same sphere

(note: thickness is
measured with
RBS)

Casimir force: skin-depth effect

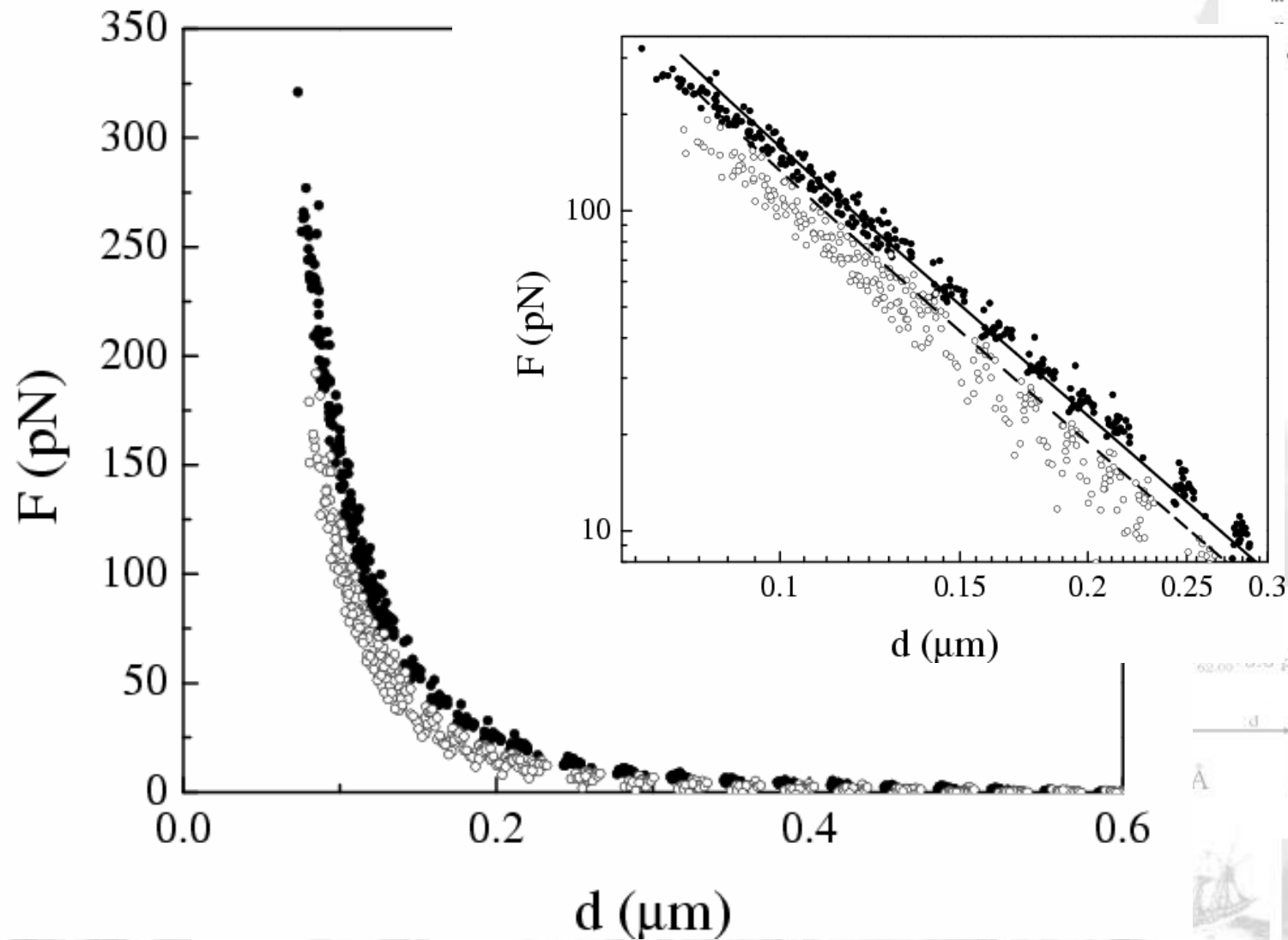


Lisanti, Iannuzzi, Capasso, PNAS **102** (2005) 11989

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Casimir force: skin-depth effect



Lisanti, Iannuzzi, Capasso, PNAS **102** (2005) 11989

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CONCLUSION 1

First evidence of the
skin-depth effect
on the Casimir force

Casimir force with H-switchable mirrors

Casimir paper: two **PERFECT CONDUCTORS**

Real materials $\epsilon(\omega)$ $\longleftrightarrow$ Boundary conditions

$\epsilon(\omega)$ $\longleftrightarrow$ F $\longrightarrow$ The Casimir force depends on which materials the interacting surfaces are made of (Lifshitz theory)

Highly reflective

Transparent

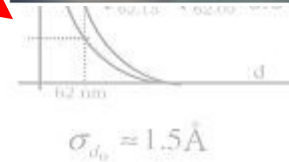
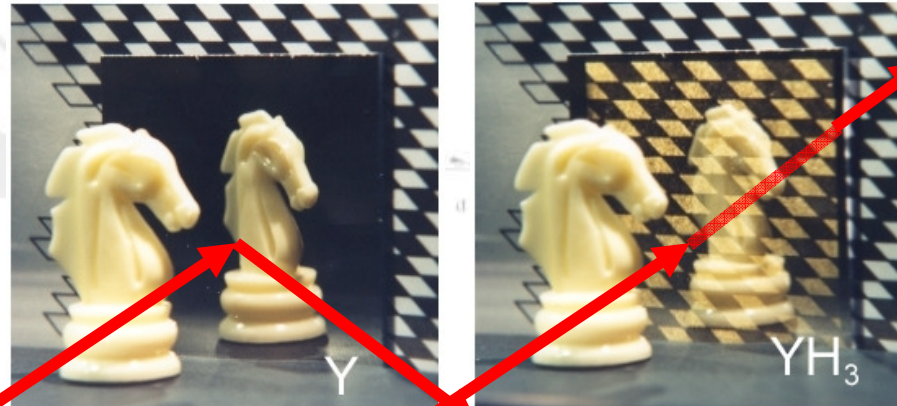
Is it possible to do it in situ?
We need **metallic** surfaces that can be **switched** from reflective to transparent!



Casimir force with H-switchable mirrors

Hydrogen Switchable Mirrors

R. Griessen, J. H. Rector
and J. Huiberts
(Vrije Universiteit)



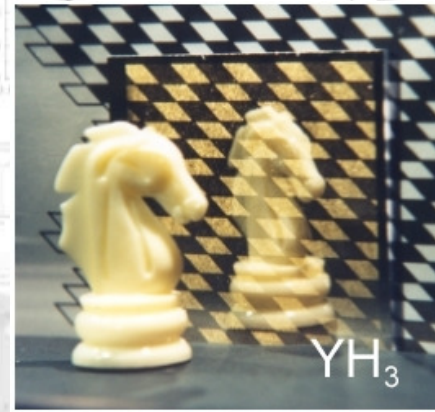
Casimir force with H-switchable mirrors

The idea: measurement of the Casimir force in air and in hydrogen

Highly reflective



Transparent



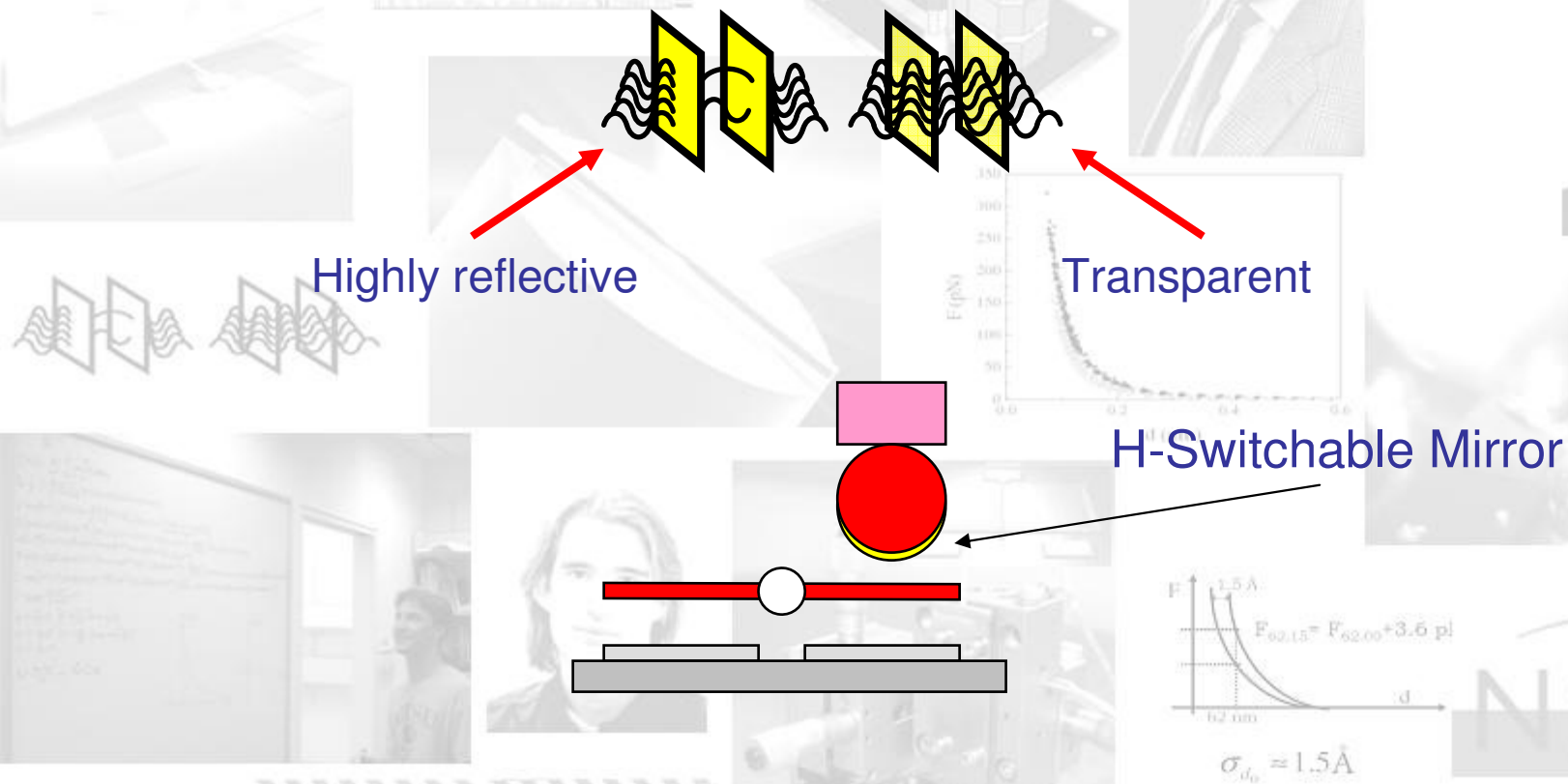
$$\sigma_{d_0} \approx 1.5 \text{ \AA}$$

The goal: tuning the Casimir force *in situ*, from strong to weak



Casimir force with H-switchable mirrors

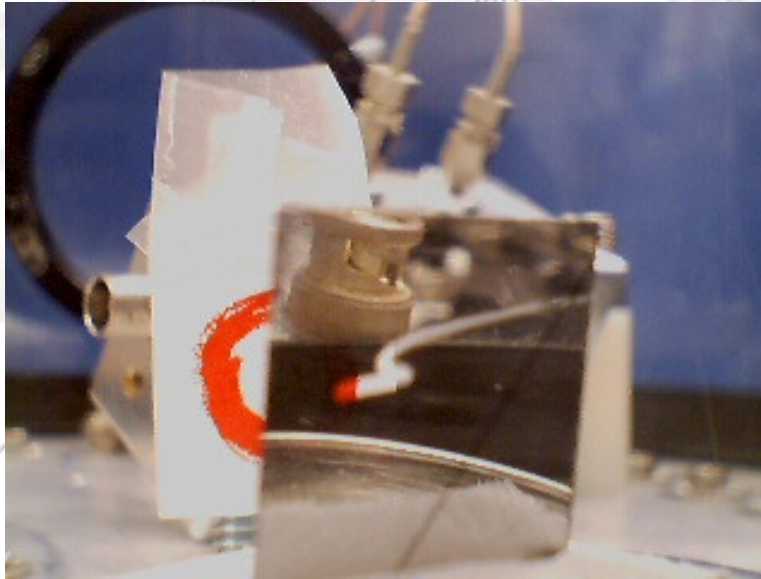
The idea: measurement of the Casimir force in air and in hydrogen



The goal: tuning the Casimir force *in situ*, from strong to weak

Casimir force with H-switchable mirrors

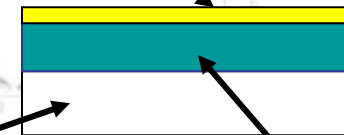
Mirror in air



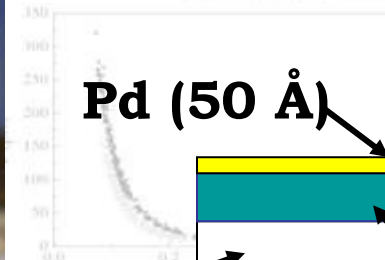
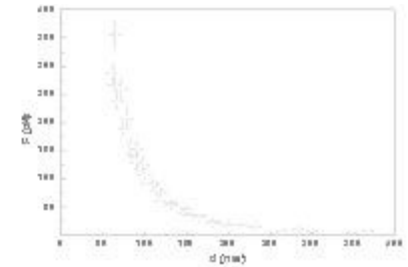
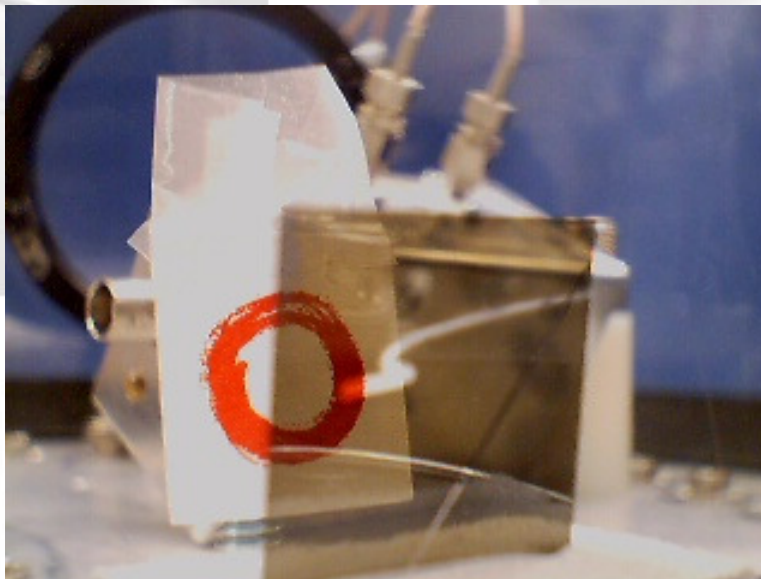
Pd (50 Å)

glass

Ni+Mg



Same mirror
in H atmosphere

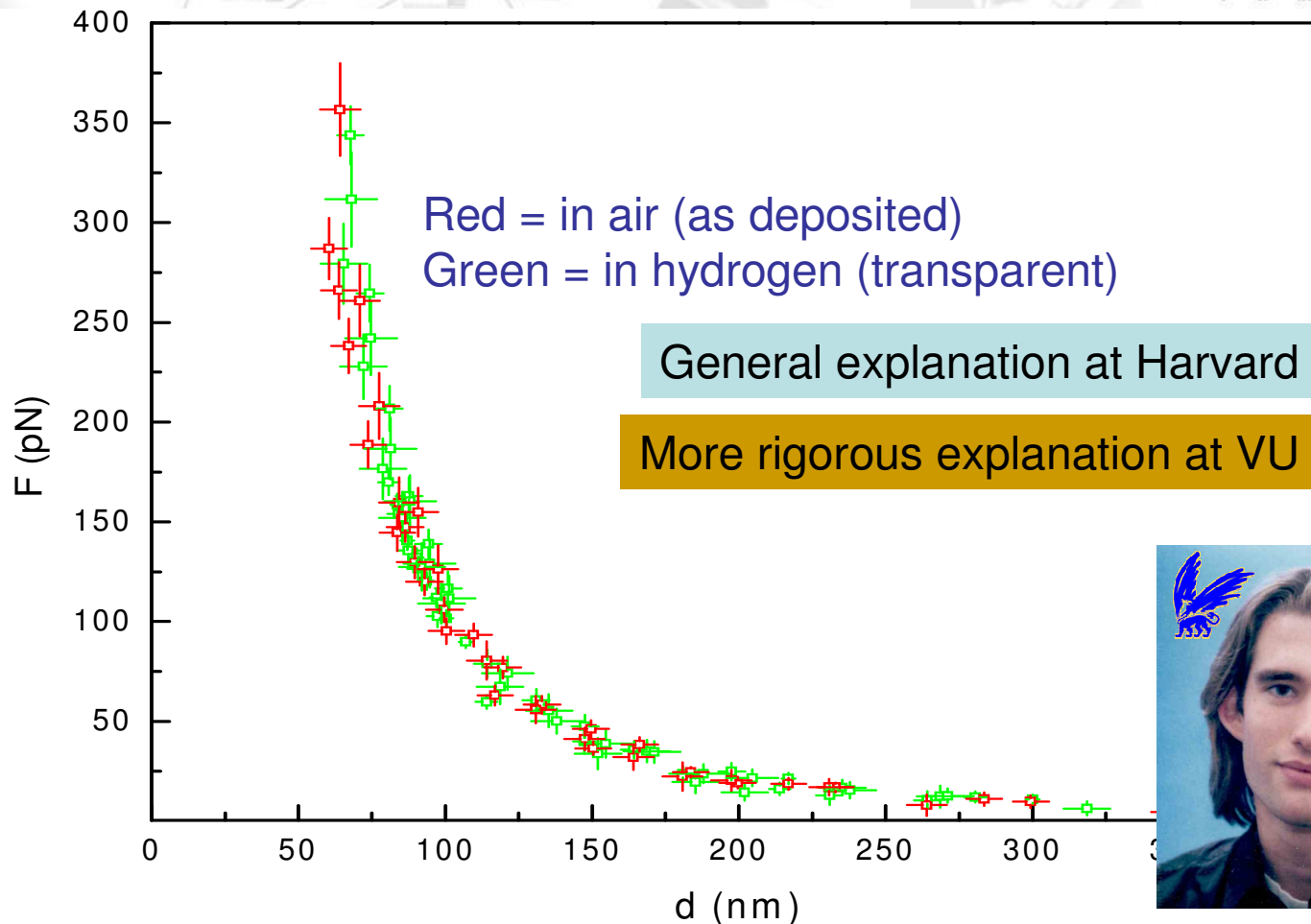


$$\sigma_{d_0} = 1.5 \text{ Å}$$
$$F = 1.5 \text{ Å}$$
$$F = 1.5 \text{ Å} + 3.6 \text{ pN}$$



Casimir force with H-switchable mirrors

Results: Why is the change below experimental sensitivity?



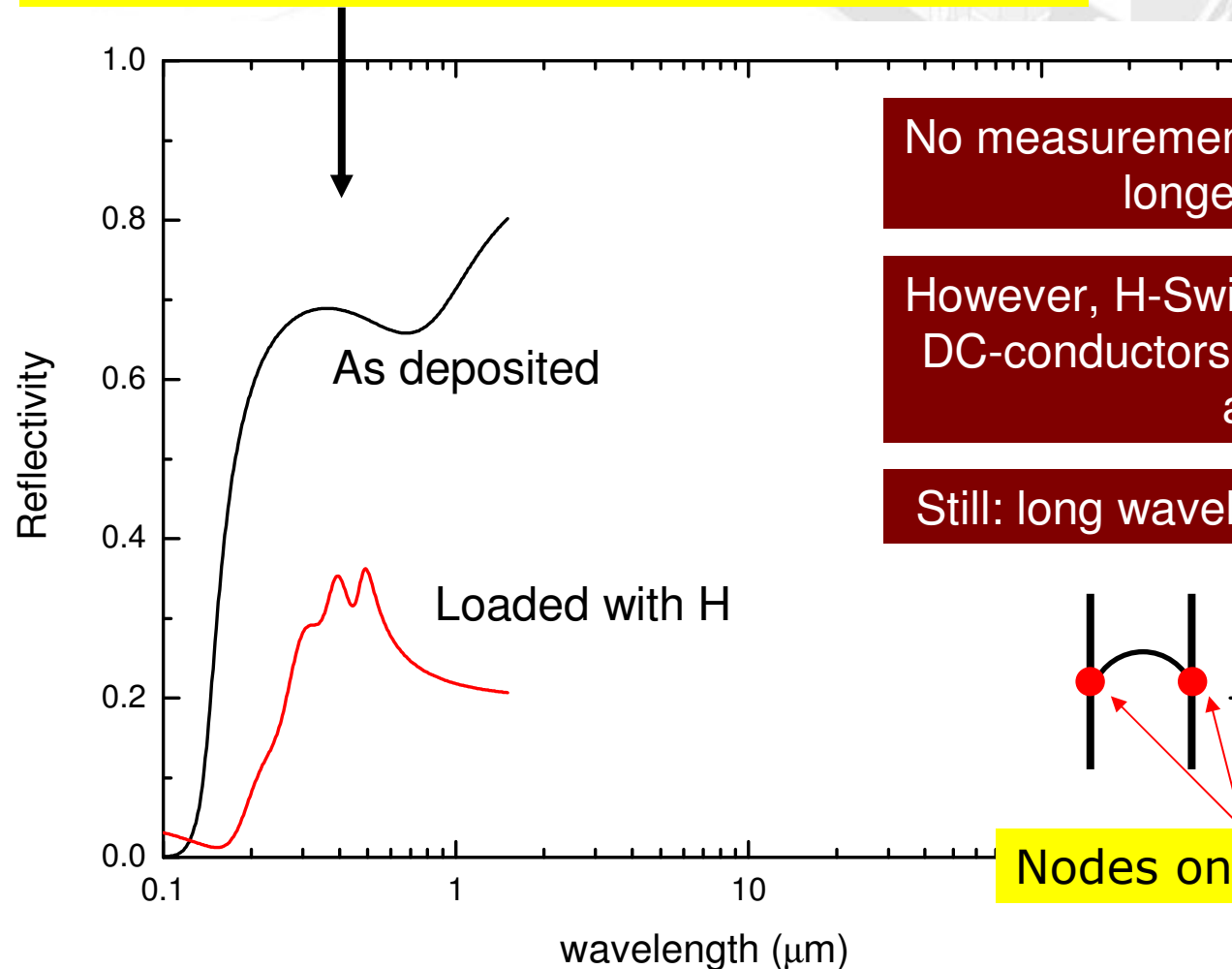
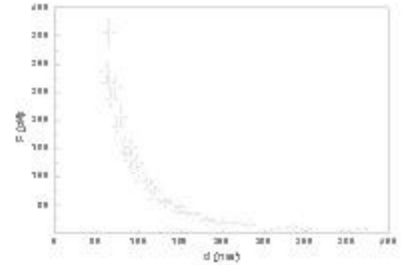
Iannuzzi, Lisanti, Capasso, *PNAS* **101** (2004) 4019

De Man, Iannuzzi, *New J. Phys.*, in press (2006)



Casimir force with H-switchable mirrors

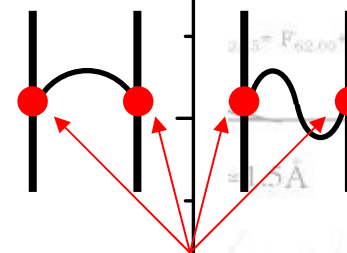
Dielectric functions of H-Switchable Mirrors are known to switch in visible and near-IR



No measurement has been performed at longer wavelengths

However, H-Switchable Mirrors are good DC-conductors. Reflectivity must go up at some λ

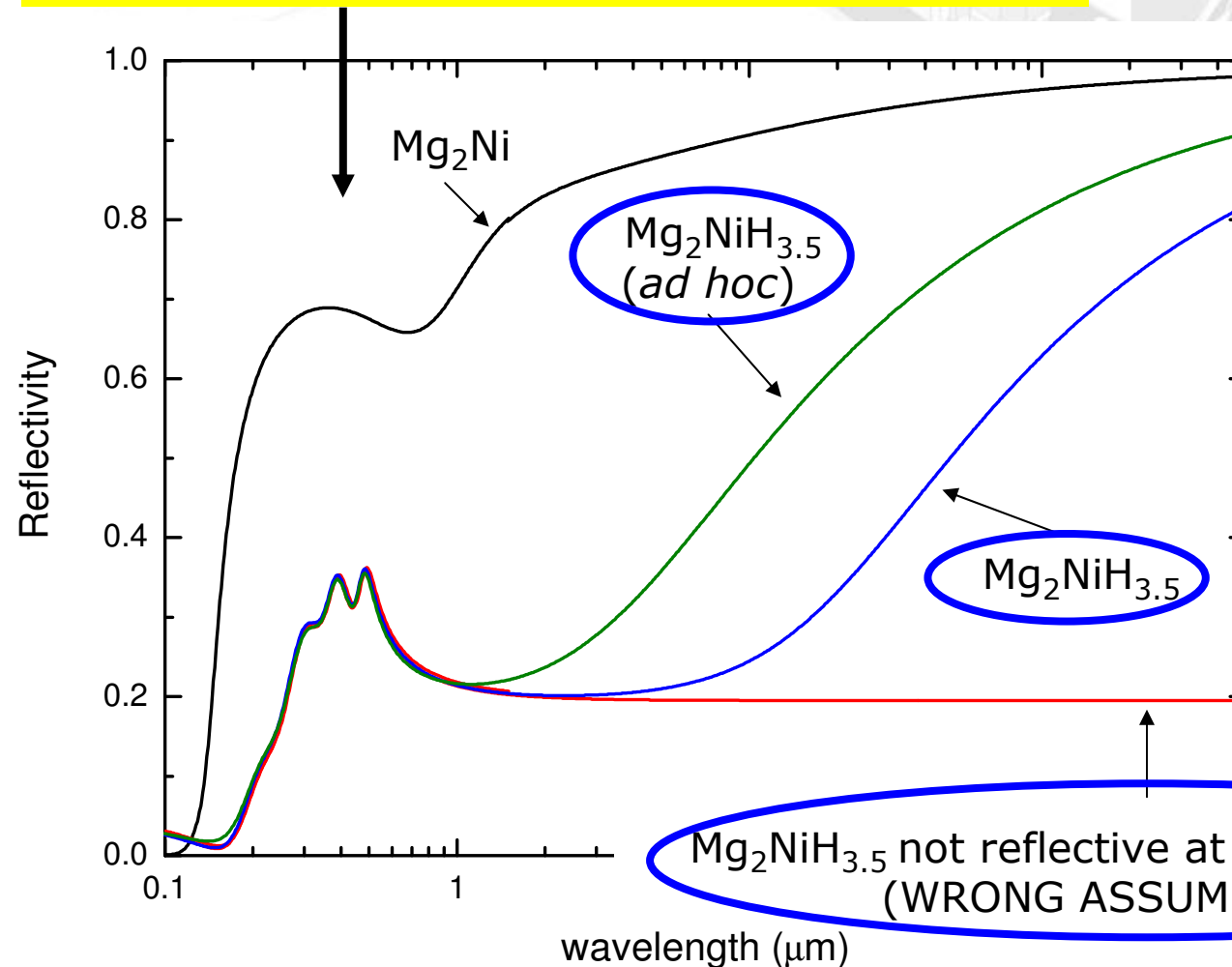
Still: long wavelengths should not count



Nodes on the plates

Casimir force with H-switchable mirrors

Dielectric functions of H-Switchable Mirrors are known to switch in visible and near-IR

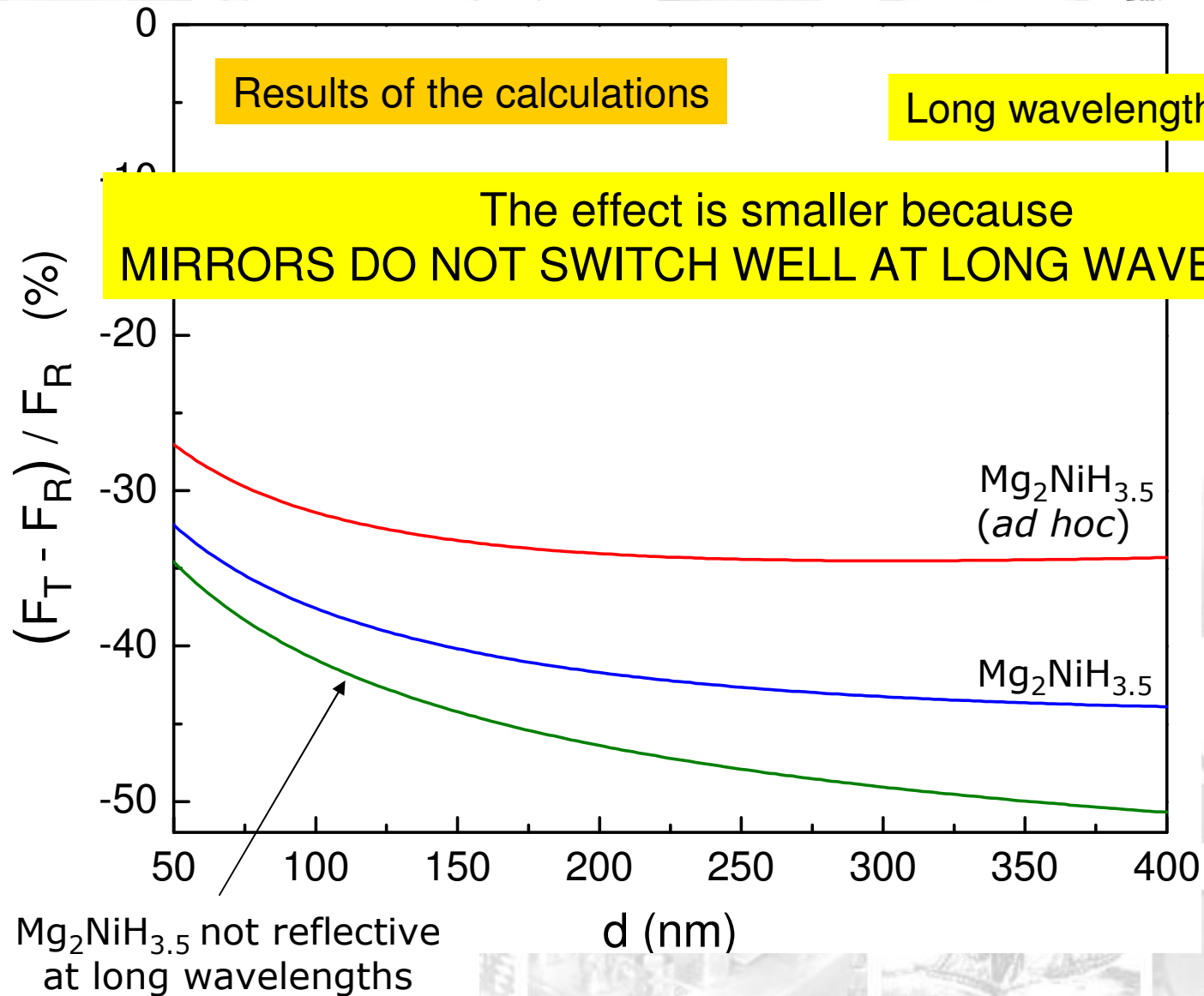


From magnetoresistance and Hall effect measurements we can extract information on long wavelengths

These three models should give the same result



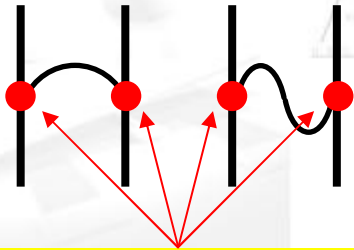
Casimir force with H-switchable mirrors



WHY?



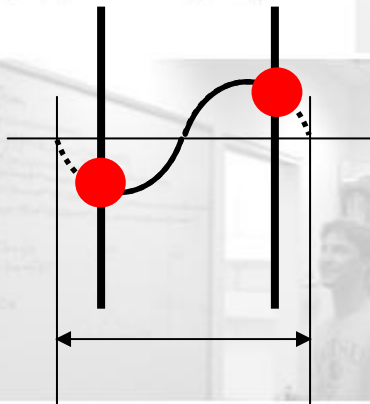
Casimir force with H-switchable mirrors



Nodes on the plates

These are the modes considered so far

This is a constraint due to the hypothesis of
PERFECT CONDUCTORS



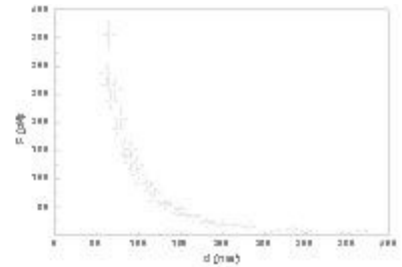
$\lambda > d$

For “real” materials:

$\epsilon(\omega)$

determines the boundary conditions

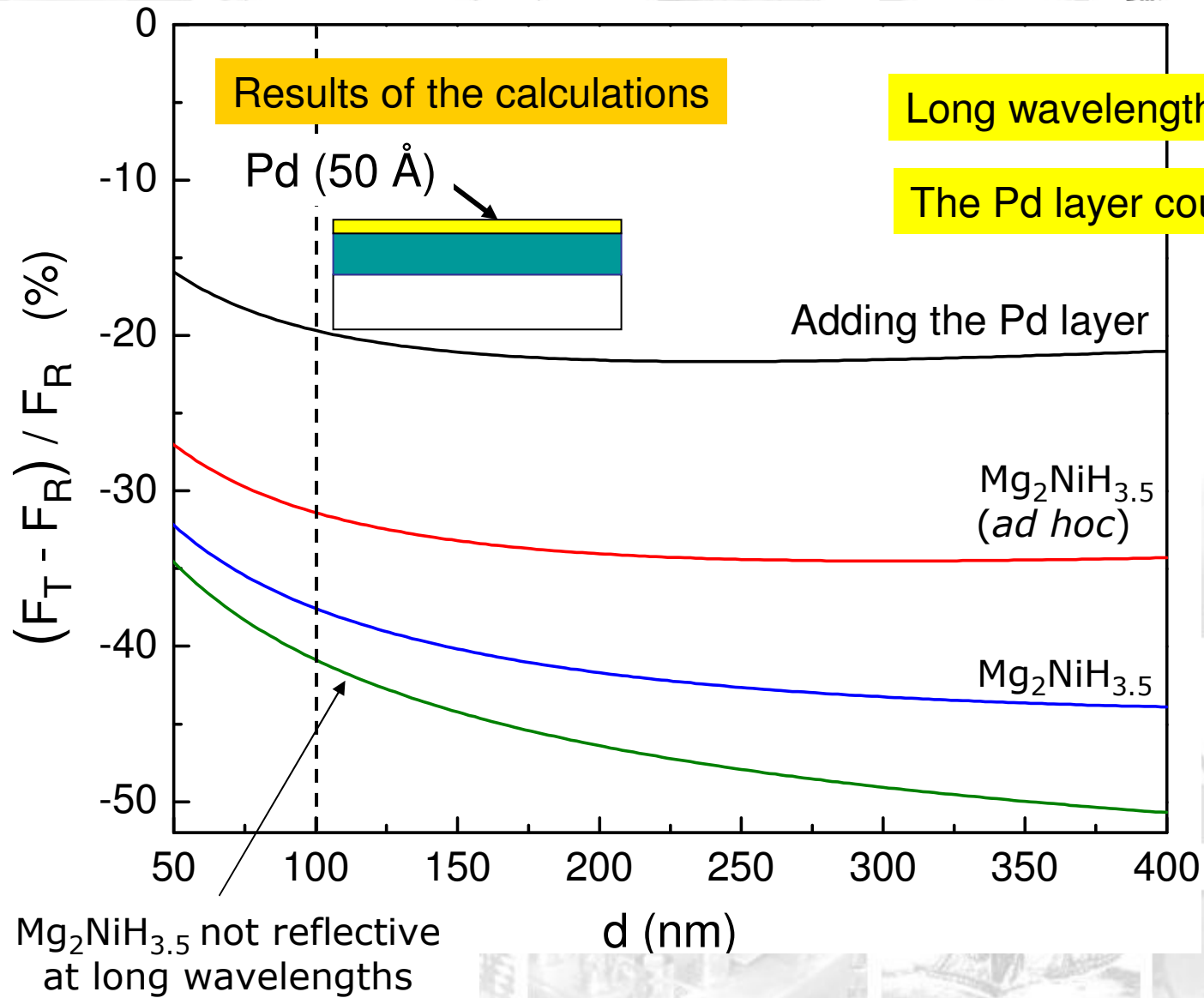
Longer wavelength modes are allowed and
will thus contribute to the force



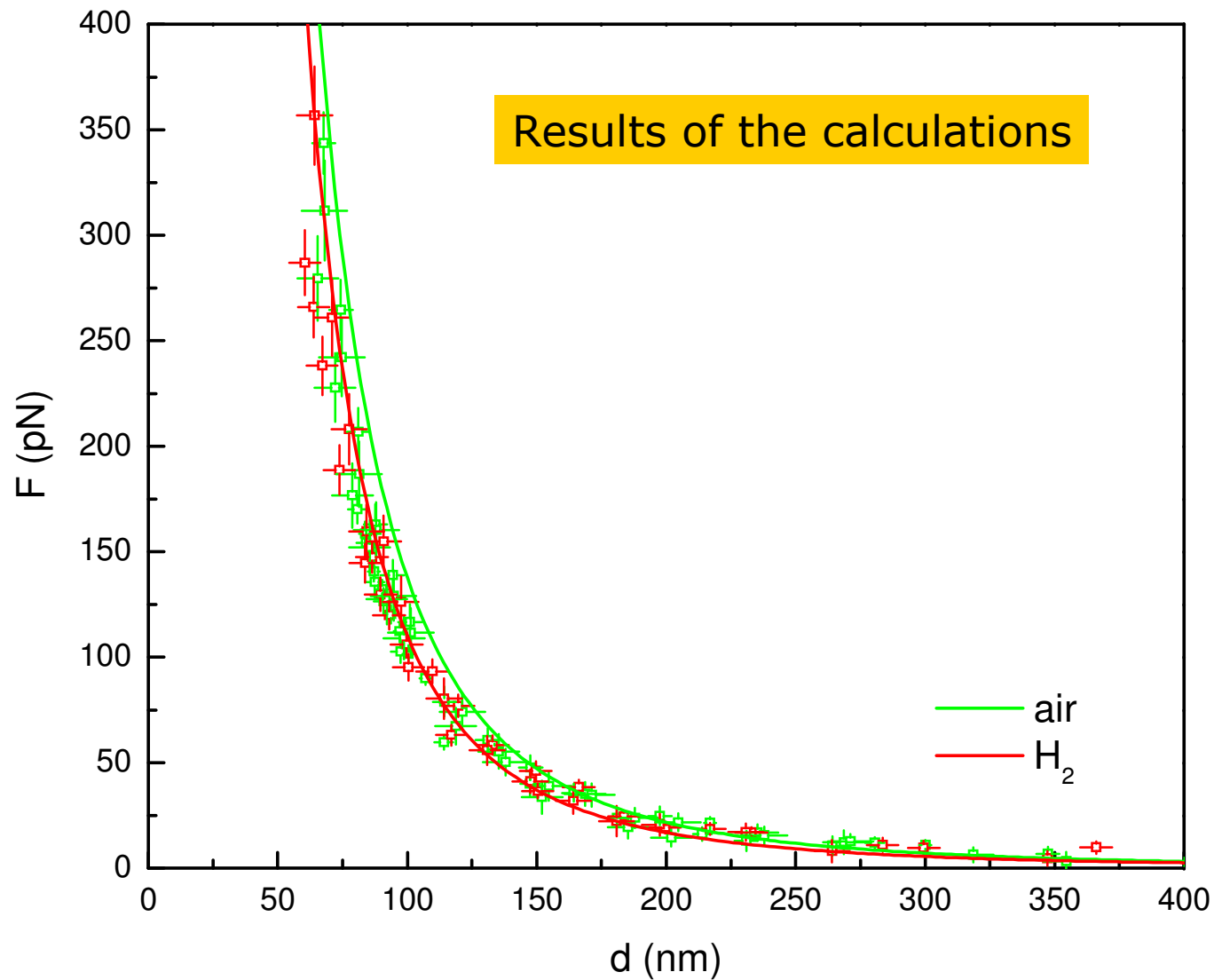
$$F_{62.15} = F_{62.00} + 3.6 \text{ pN}$$



Casimir force with H-switchable mirrors



Casimir force with H-switchable mirrors



CONCLUSION 2

Hydrogen Switchable Mirrors offer the possibility to tune the Casimir force

First experiment: no effect observed

Reasons:
long wavelengths count
thin metallic layers count

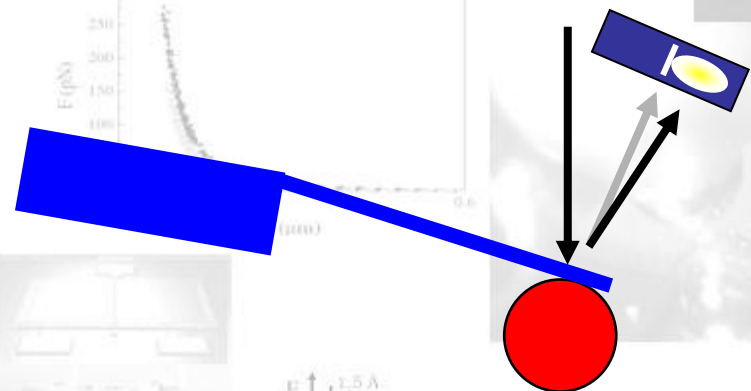
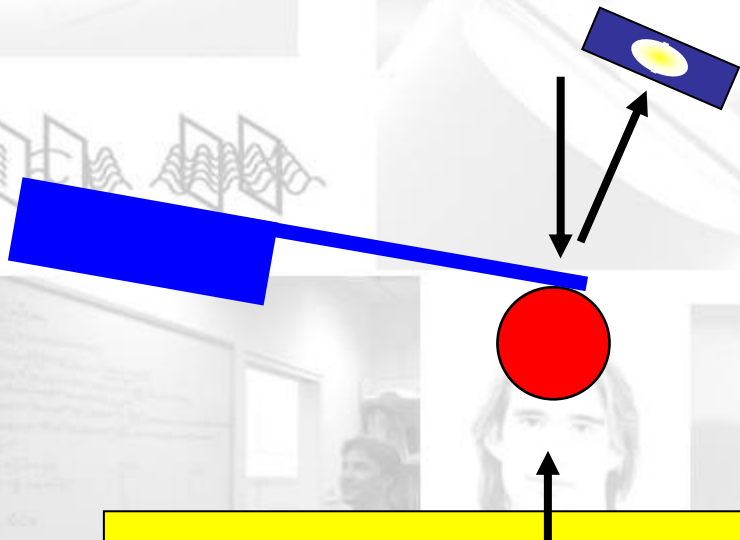
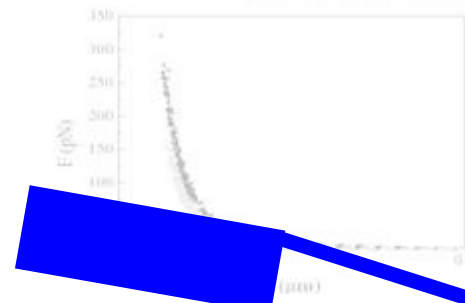
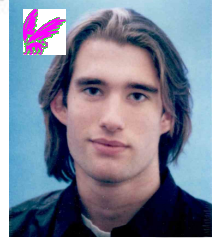
Effects at 20% expected (should be measurable)

Game is not over

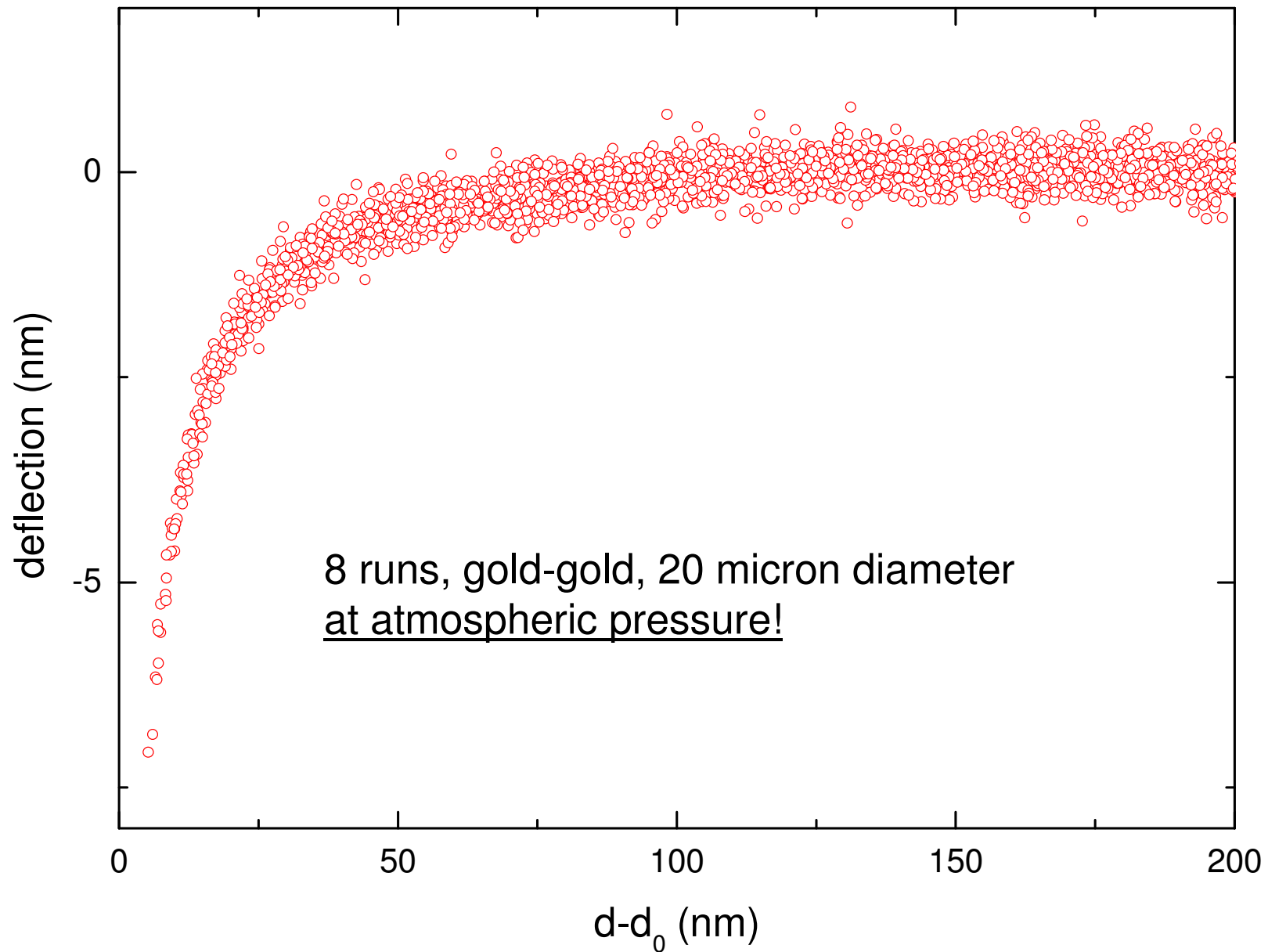
Casimir force with H-switchable mirrors II

Casimir force with H-Switchable Mirrors Episode II

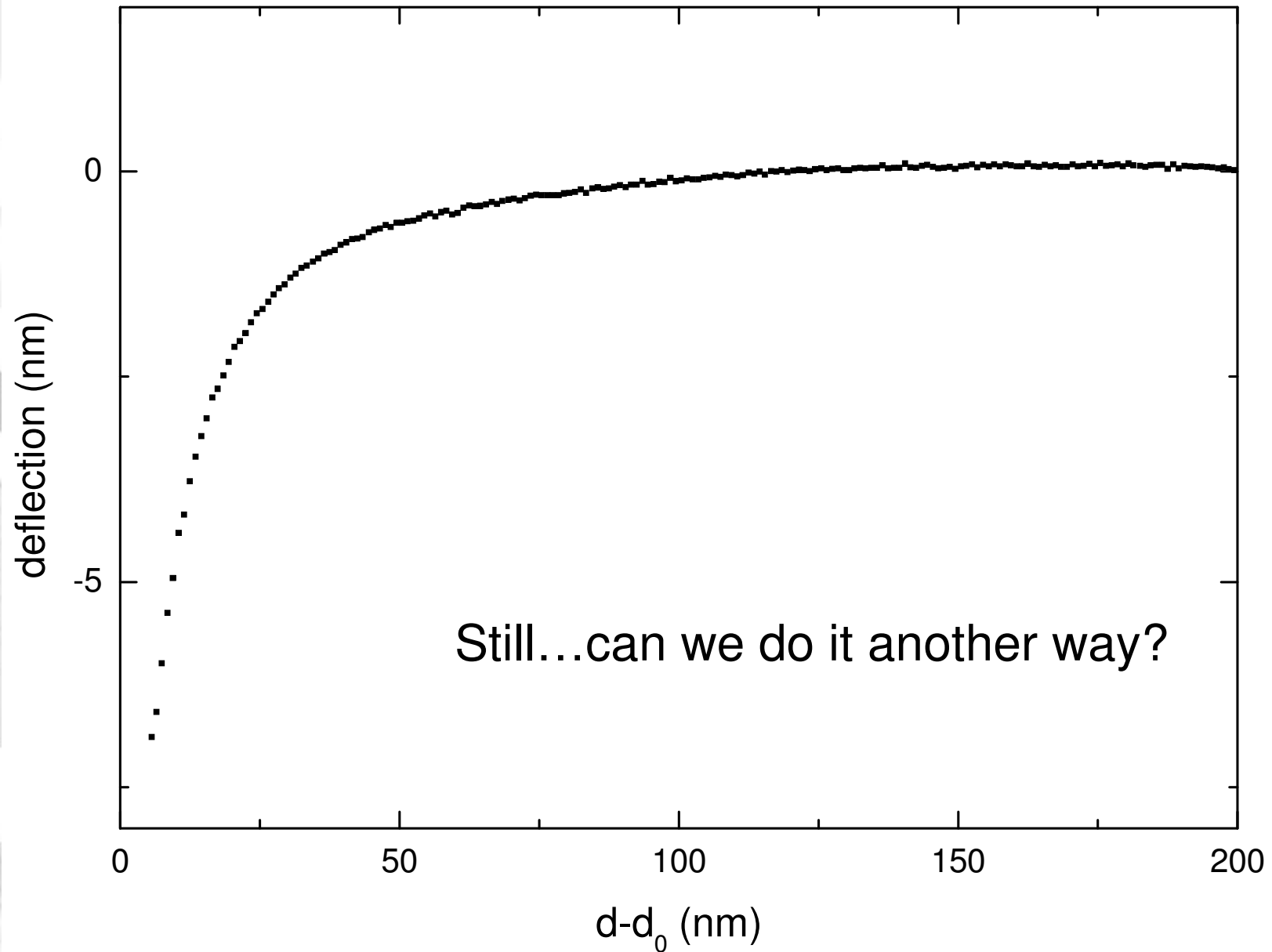
“Warming-up” with an atomic force microscope



Casimir force with H-switchable mirrors II



Casimir force with H-switchable mirrors II



A new Casimir setup: let's get to work...

Single mode
optical fiber

125 μm

A new sensor for Casimir experiments and...

A conceptually new Casimir force apparatus (...and much more than that !)



K. Heeck, J.H. Rector, H. Schreuders, M. Slaman



Szabolcs Deladi



Miko Elwenspoek

Iannuzzi et al., Appl. Phys. Lett. **88** (2006) 053052

Deladi et al., J. Micromech. Microeng. **16** (2006) 886

Iannuzzi et al., Rev. Sci. Instr. **77** (2006) 106105

Iannuzzi et al., OSF-18 Technical Digest (2006) TuB2

Iannuzzi et al., accepted for publication in Sensors & Act. **B** (2006)

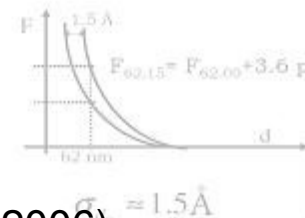
Iannuzzi et al., accepted for publication in Optics & Photonics News (2006)

2006 Rhenaphotonics Alsace Best Design Award

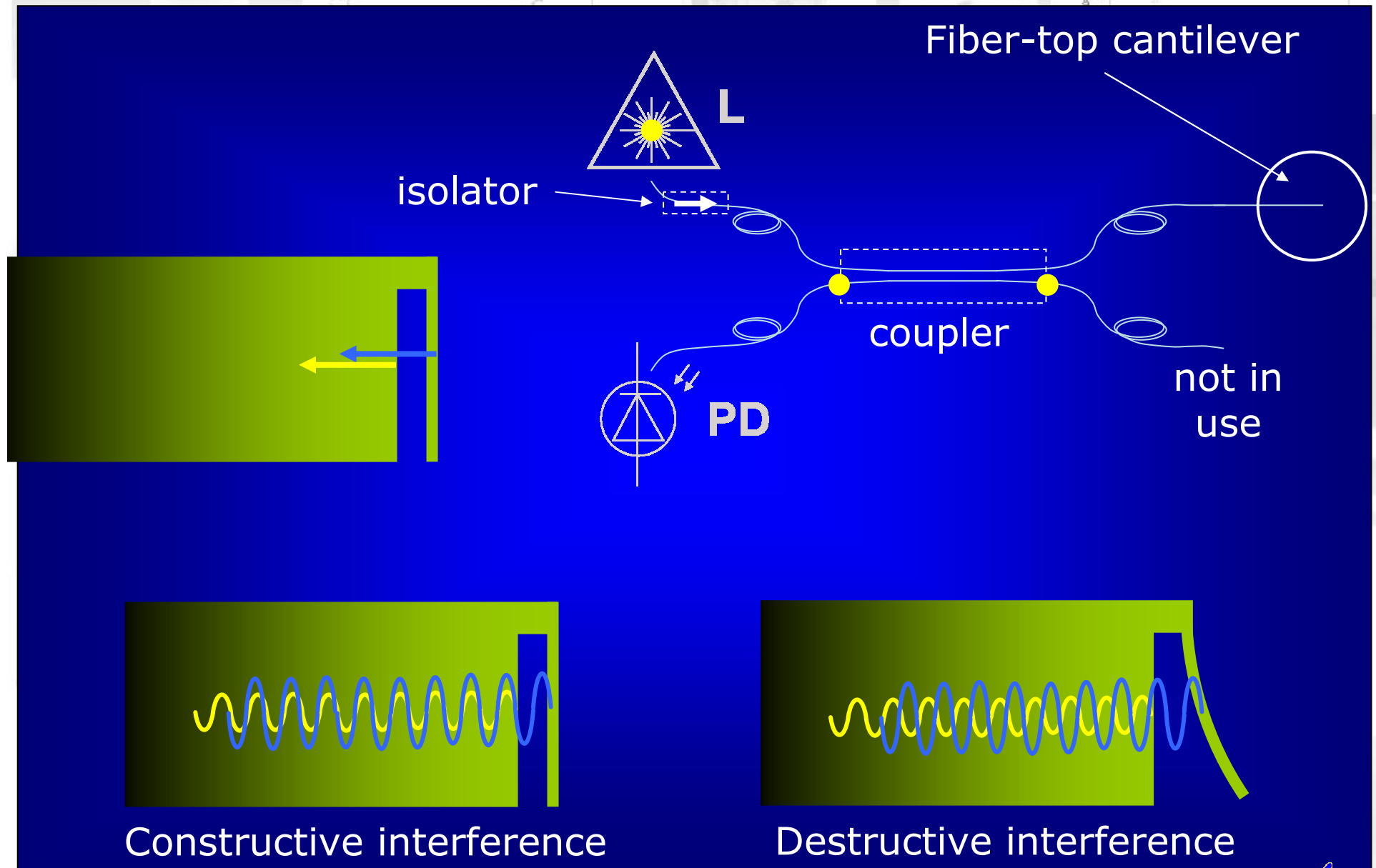
2006 Rhenaphotonics Alsace Best Technology Award

Iannuzzi, Deladi, Elwenspoek, patent PCT/NL2005/000816 (filed)

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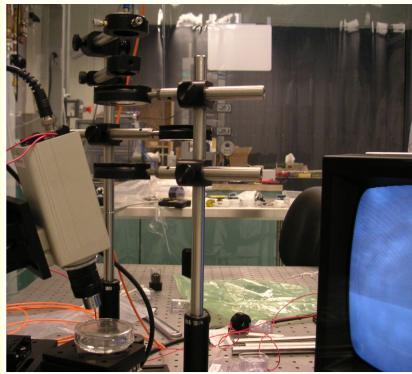


A new sensor for Casimir experiments and...



A new sensor for Casimir experiments and...

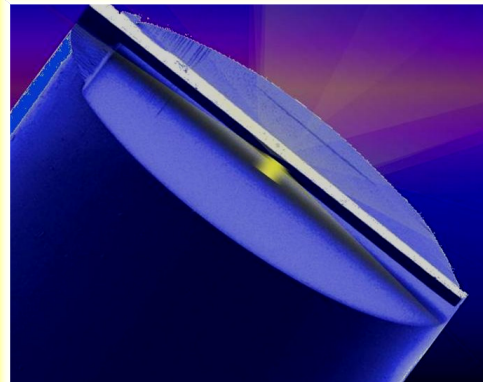
Research
laboratories



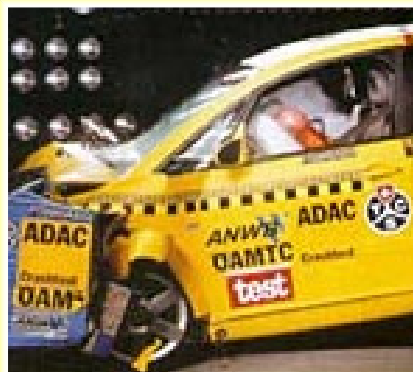
Space missions



Homeland security



Quality inspection



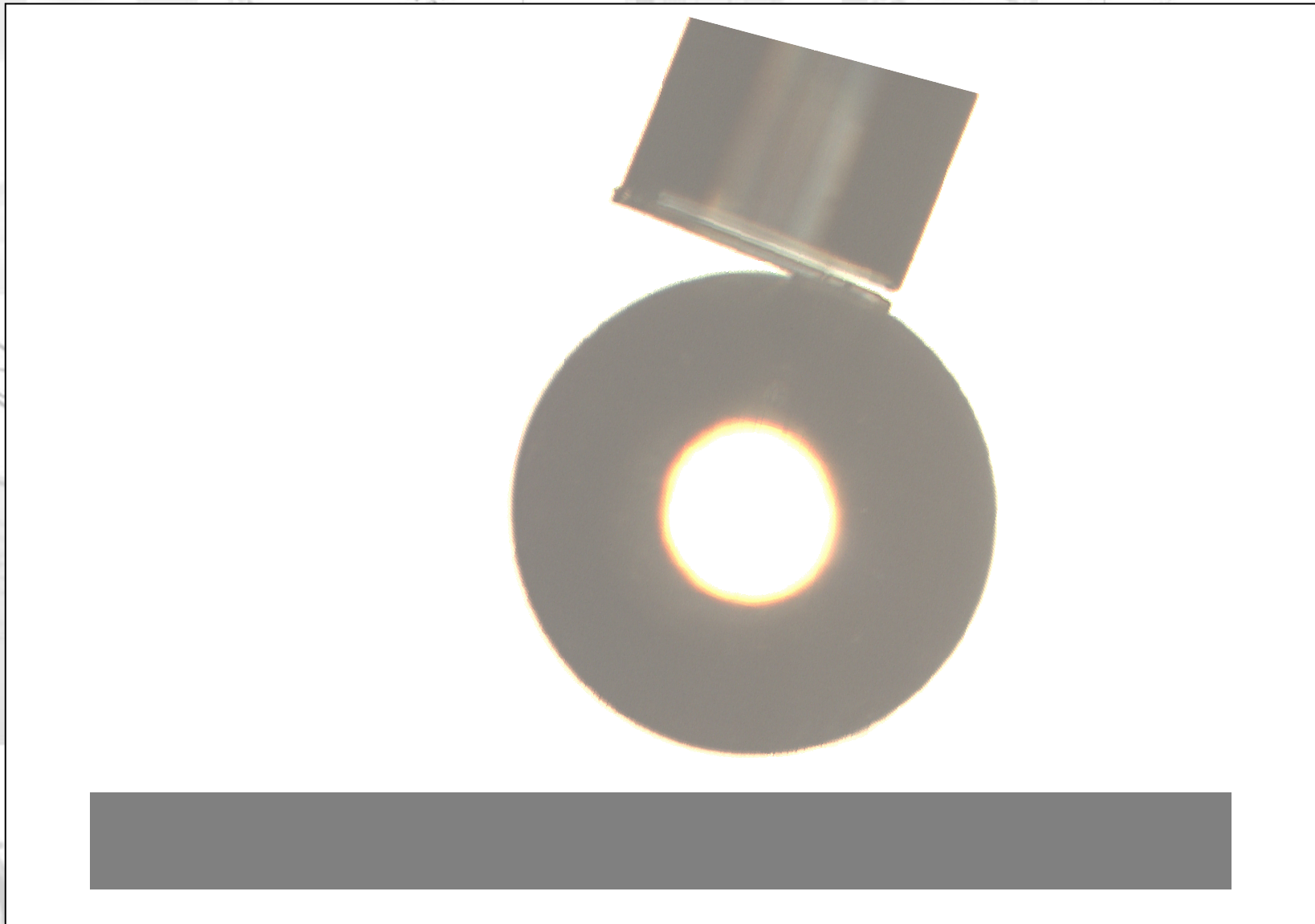
Surgery rooms &
medical applications



Environmental
analysis



A new sensor for Casimir experiments

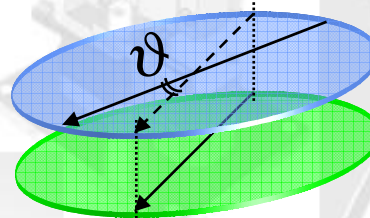


CONCLUSION 3

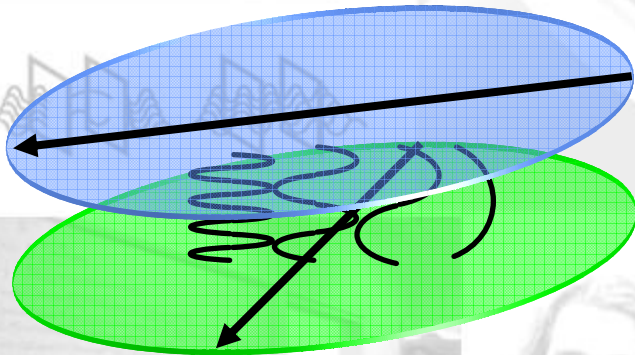
We have developed a new sensor for multipurpose applications, among which Casimir force measurements in vacuum, gases, and liquids.

Quantum electrodynamical torque

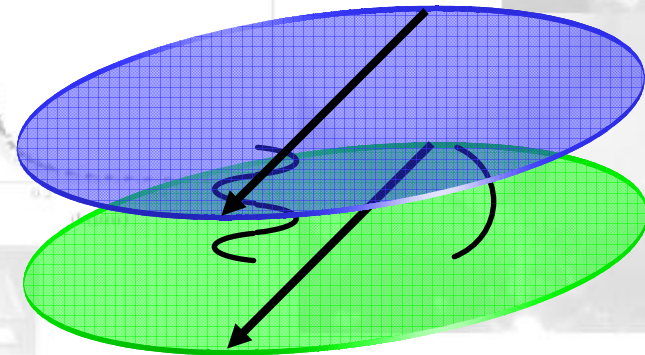
Birefringent materials: reflection, absorption, transmission depend on orientation



Zero-point energy depends on the orientation too!



$$M = -\frac{\partial E}{\partial \vartheta}$$



V. A. Parsegian and G. H. Weiss, *J. Adhesion* **3** (1972) 259 (non-retarded limit)
Y. Barash, *Izvestiya vuzov, Radiofizika*, Tom **XXI** (1978) 1637

Quantum Electrodynamical torque



Quantum electrodynamical torque

A simplified equation (non-retarded, slightly birefringent materials)

$$M = -\frac{\hbar \bar{\omega} \sin 2\theta}{64\pi^2 d^2} A$$

$$\bar{\omega} = \int_0^\infty d\omega \frac{-(\epsilon_1 - \epsilon_2)^2}{(1 + \epsilon_2)^2 (1 - \epsilon_2)^2} \ln \left(1 - \left(\frac{1 - \epsilon_2}{1 + \epsilon_2} \right)^2 \right)$$

Important features

$$M \propto \frac{1}{d^2}$$

Small separations
are necessary

$$M \propto A$$

Area of the surfaces
must be relatively large

$$M \propto \sin 2\theta$$

Strong signature

Can help to
distinguish spurious
effects

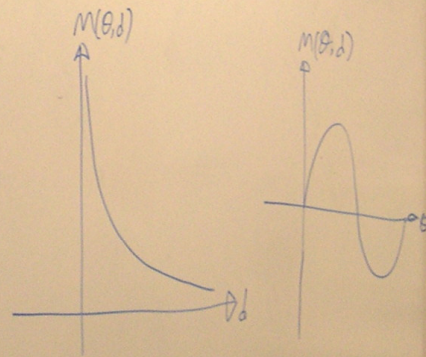
Make the experiment difficult
(surfaces tend to come into
contact)

The complete equation?

Quantum electrodynamical torque

The complete equation!!!

$$\begin{aligned} \vec{p} &= -\frac{\partial \mathcal{L}}{\partial \vec{S}} \\ \vec{S}(\vec{p}, d) &= \frac{k_B T}{4\pi^2} \sum_{n=0}^{\infty} \int_0^{2\pi} \int_0^{2\pi} d\Omega \, D_n(\vec{p}, \Omega) d\vec{p} \\ \Delta_m &= \frac{1}{8} \cdot \left(A \frac{(\vec{p}_1 - \vec{p}_2) \cdot \vec{\epsilon}_{1,2}^{(n)}}{p_1^2 - \epsilon^2 \sin^2(\varphi + \vartheta)} \left[B \vec{\epsilon}_{1,2}^{(n)}(\varphi + \vartheta) - E \left[2 \vec{\epsilon}_{1,2}^{(n)} \cos \vartheta \sin(\varphi + \vartheta) + p_1^2 \sin^2 \vartheta \right] \right] \right\} \\ \vec{p} &= (\vec{p}_1 + \vec{p}_2) / (\vec{p}_1 + \vec{p}_2) \cdot \left\{ (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 + \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) - \frac{\vec{\epsilon}_{1,2}^{(n)} (\vec{p}_1 - \vec{p}_2) \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2)}{p_1^2 - \epsilon^2 \sin^2 \varphi} \right\} \\ A &= \left\{ (\vec{p}_1 + \vec{p}_2) \cdot (\vec{p}_1 + \vec{p}_2) - (\vec{p}_1 \cdot \vec{p}_1) (\vec{p}_2 \cdot \vec{p}_2) e^{-2\varphi} \right\} \cdot \left\{ (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 + \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 + \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) - \frac{\vec{\epsilon}_{1,2}^{(n)} (\vec{p}_1 - \vec{p}_2) \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2)}{p_1^2 - \epsilon^2 \sin^2 \varphi} \right\} \\ &+ 2(\vec{\epsilon}_{1,2}^{(n)} - \vec{\epsilon}_{1,2}^{(n)}) \left[\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_2 + \vec{p}_1 \vec{p}_2) + \vec{p}_1 \vec{p}_2 \cdot (\vec{\epsilon}_{1,2}^{(n)} - \vec{\epsilon}_{1,2}^{(n)}) \vec{p}_1 \right] e^{-2\varphi} + (\vec{\epsilon}_{1,2}^{(n)} + \vec{p}_1 \vec{p}_2) (\vec{\epsilon}_{1,2}^{(n)} - \vec{\epsilon}_{1,2}^{(n)}) (\vec{p}_1 \cdot \vec{p}_2) e^{-2\varphi} \\ B &= \left\{ (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 + \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) \cdot (\vec{p}_1 + \vec{p}_2) + 2(\vec{\epsilon}_{1,2}^{(n)} - \vec{\epsilon}_{1,2}^{(n)}) (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) e^{-2\varphi} \right\} \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) (\vec{p}_1 \cdot \vec{p}_2) e^{-2\varphi} + \frac{(\vec{p}_1 + \vec{p}_2) \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2)}{p_1^2 - \epsilon^2 \sin^2 \varphi} \cdot \left[(\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) + \right. \\ &\left. + (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) \cdot (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) \right] \\ C &= \vec{p}_1 \vec{p}_2 \cdot \left\{ -(\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 + \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) (\vec{p}_1 + \vec{p}_2) + \vec{p}_1 (\vec{\epsilon}_{1,2}^{(n)} - \vec{\epsilon}_{1,2}^{(n)}) (\vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) e^{-2\varphi} + \frac{(\vec{p}_1 - \vec{\epsilon}_{1,2}^{(n)} \vec{p}_2) (\vec{p}_1 \cdot \vec{p}_2) e^{-2\varphi}}{p_1^2 - \epsilon^2 \sin^2 \varphi} \right\} \\ E &= 4 \vec{p}_1 \vec{p}_2 \cdot \frac{(\vec{p}_1 - \vec{p}_2) \cdot \vec{\epsilon}_{1,2}^{(n)}}{p_1^2 - \epsilon^2 \sin^2 \varphi} e^{-2\varphi} \\ p_1^2 &= \vec{p}_1^2 - \frac{\sum_{i=1}^L \epsilon_{1,i}^{(n)}}{c^2} \epsilon_{1,2}^{(n)} \quad \left| \quad \vec{p}_1^2 = \vec{p}_1^2 \left(\frac{\epsilon_{1,2}^{(n)}}{\epsilon_{1,1}^{(n)}} - 1 \right) \vec{\epsilon}_{1,2}^{(n)} \vec{p}_1 - \frac{\sum_{i=1}^L \epsilon_{1,i}^{(n)}}{c^2} \epsilon_{1,2}^{(n)} \right. \\ p_2^2 &= \vec{p}_2^2 - \frac{\sum_{i=1}^L \epsilon_{2,i}^{(n)}}{c^2} \epsilon_{2,2}^{(n)} \quad \left| \quad \vec{p}_2^2 = \vec{p}_2^2 \left(\frac{\epsilon_{2,2}^{(n)}}{\epsilon_{2,1}^{(n)}} - 1 \right) \vec{\epsilon}_{2,2}^{(n)} \vec{p}_2 - \frac{\sum_{i=1}^L \epsilon_{2,i}^{(n)}}{c^2} \epsilon_{2,2}^{(n)} \right. \\ p_3^2 &= \vec{p}_3^2 - \frac{\sum_{i=1}^L \epsilon_{3,i}^{(n)}}{c^2} \epsilon_{3,3}^{(n)} \\ \vec{S}_m &= \frac{2\pi \cdot k_B T}{h} \cdot m \cdot \vec{\epsilon}_{1,2}^{(n)} \cdot \vec{\epsilon}_{1,2}^{(n)} (\vec{p}_1) \end{aligned}$$

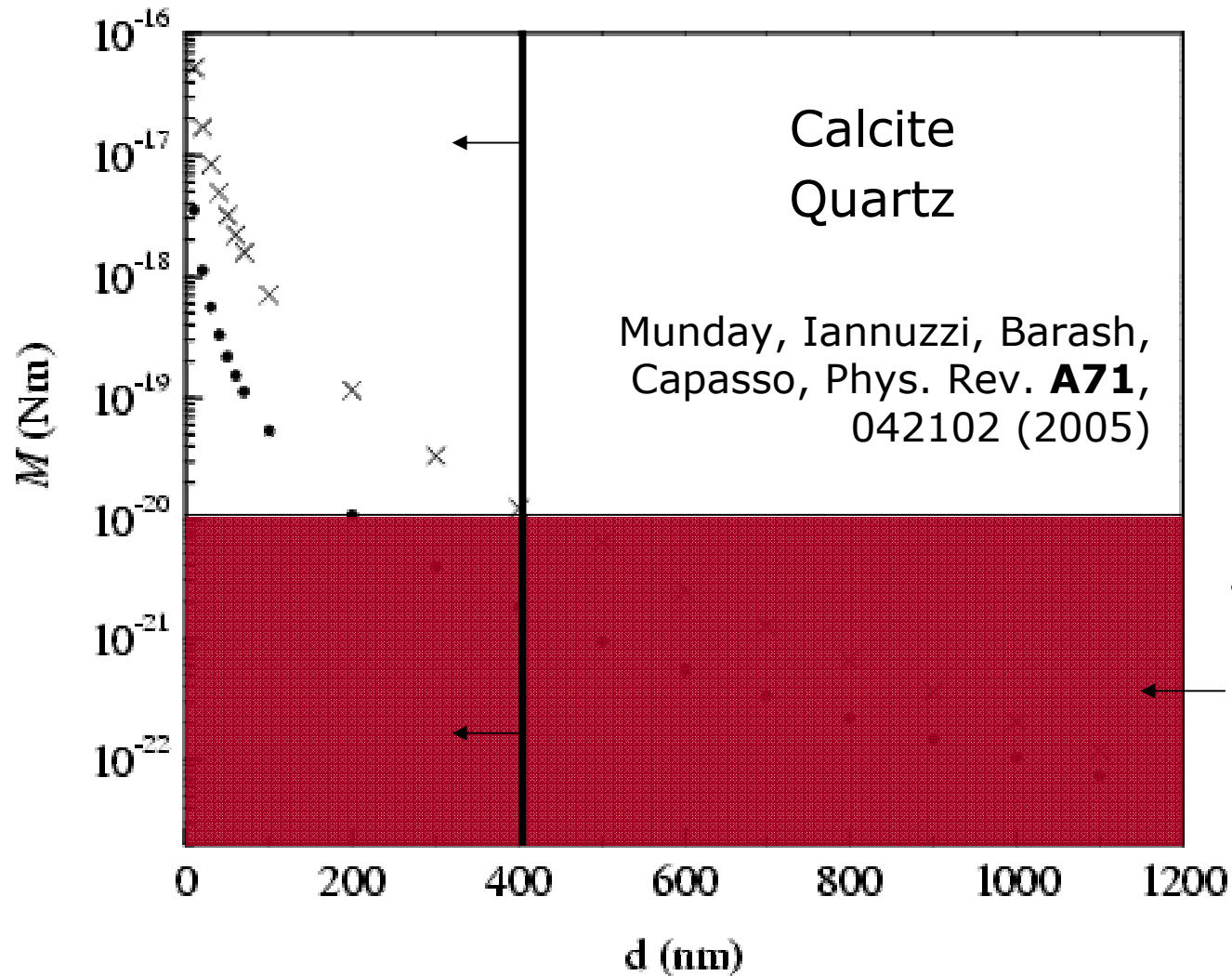


Jeremy N. Munday



Quantum electrodynamical torque

Quartz or calcite disk ($\varnothing=40\mu\text{m}$, $t=20\mu\text{m}$) on top of barium titanate



Bad news

Quite a technical
challenge!

The effect is too small
for currently available
technologies



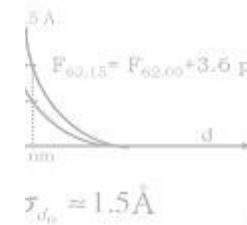
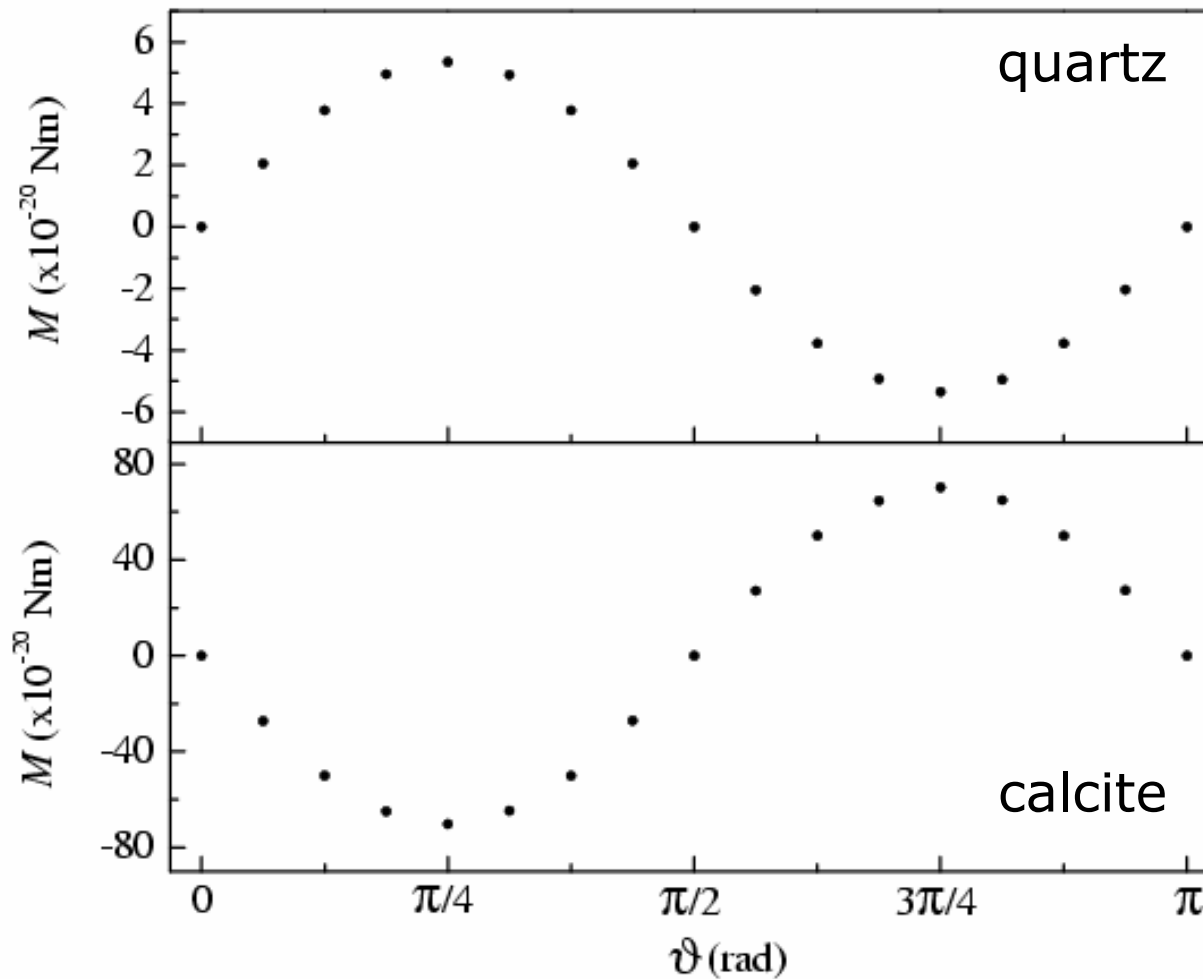
Quantum electrodynamical torque

Quartz or calcite disk ($\varnothing=40\mu\text{m}$, $t=20\mu\text{m}$) on top of barium titanate

Good news

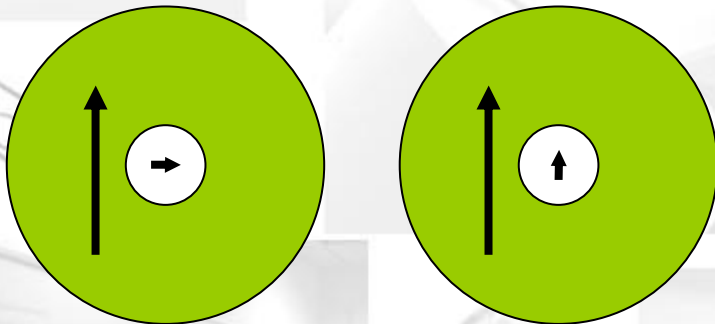
Torque versus angle for
 $d = 100 \text{ nm}$

$$M \propto \sin 2\theta$$



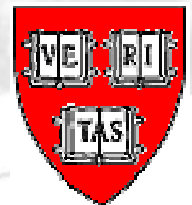
Quantum electrodynamical torque

- Smaller surfaces: a better choice?
- Let's take a small disk ($\varnothing < 1 \mu\text{m}, t \sim 100\text{nm}$)

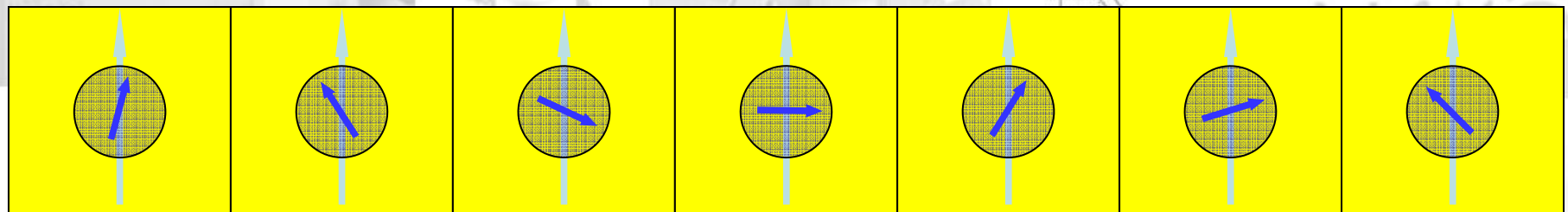


$$E(\pi/2) - E(0) \approx k_B T$$

Itan Barmes



Still in collaborations with



$t=0$

$t=t_0$

$t=2t_0$

$t=3t_0$

$t=4t_0$

$t=5t_0$

$t=5t_0$

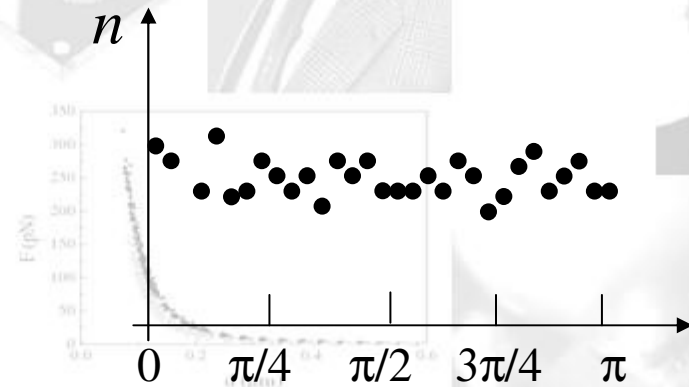
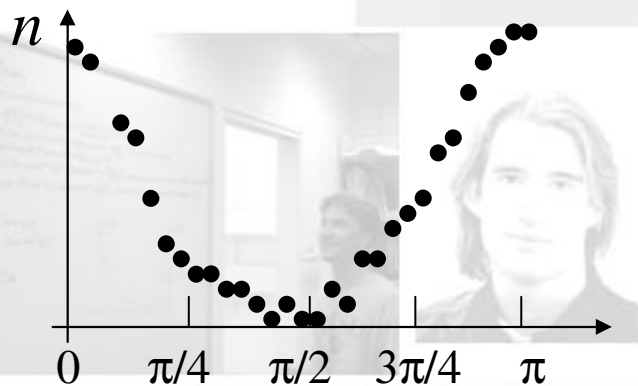


Quantum electrodynamical torque

Measure the position as a function of time

If energy did not depend on θ

But energy depends on θ



$$p(\vartheta) \propto \exp\left(-\frac{E(\vartheta)}{k_B T}\right)$$

$$\sigma_{d_0} = 1.5 \text{ \AA}$$



CONCLUSION 4

Quantum electrodynamical torque: an interesting phenomenon that has not received adequate attention

Rotation is weak: tricks are needed

One possible solution: Brownian motion

Experiment running at Harvard



CONCLUSIONS

There is plenty of room...

...beyond the accuracy issue!

Thank you for your kind attention
iannuzzi@few.vu.nl

